

# CMS Draft Analysis Note

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## Transverse Momentum Distribution within Jets in pp Collisions at $\sqrt{s}=7$ TeV

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### Abstract

Using  $pp$  collisions at center of mass energy of 7 TeV collected by CMS detector at Large Hadron Collider at CERN, we have measured the jet shapes, defined as the fractional transverse momentum distribution as a function of the distance from the jet axis. Since jet shapes are sensitive to parton showering processes they provide a good test of Monte Carlo event simulation programs. In this note we present a study of jet shapes reconstructed using calorimeter energies using CMS dataset with  $1 \text{ pb}^{-1}$  of integrated luminosity. We compare the results with predictions of the QCD inspired event generators PYTHIA and HERWIG++. For Pythia predictions, various underlying event tunes were studied. The **CW tune** described the data best.

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## 1 Introduction

The transverse momentum profile of a jet, jet shapes [1, 2], is sensitive to multiple parton emissions from the primary outgoing parton and provides a good test of the parton showering description of Quantum Chromodynamics (QCD), the theory of strong interactions. Historically the jet shape has been used to test perturbative QCD (pQCD)  $\alpha_s^3$  calculations [3, 4]. These leading order calculations, with only one additional parton in a jet, showed good agreement with the observed jet shapes. While confirming the validity of pQCD calculations, jet shape studies also indicated that jet clustering, underlying event contribution and hadronization effects must be considered. Currently, these effects can be modeled accurately only within the framework of full-event generators. Current Monte Carlo (MC) event generators use pQCD inspired parton shower models, in conjunction with hadronization and underlying event models, to generate final state particles. MC generators are used extensively to model signal and background events in most analyses at hadron colliders. Jet shapes can be used to tune phenomenological parameters in these MC generators. QCD predicts broader gluon jets than quark jets. The structure of quark and gluon jets can be investigated by comparing measurements of the jet shapes in different processes enriched with either quark or gluon initiated jets in the final state.

44 In QCD jet production, the gluon jet contribution changes with the transverse momenta of the  
 45 jets. Previously, jet shapes have been measured in  $p\bar{p}$  collisions at Tevatron and  $ep$  collisions at  
 46 HERA [3–7]. In this paper, we present a study of jet shapes measured using calorimeter infor-  
 47 mation in the central region of the CMS detector at  $\sqrt{s} = 7$  TeV using integrated luminosity of  
 48  $1.0 \text{ nb}^{-1}$ . and compare the results obtained with various MC generators. The sensitivities of  
 49 jet shapes to the underlying event (UE) model and to the flavor of the initiating parton are also  
 50 explored.

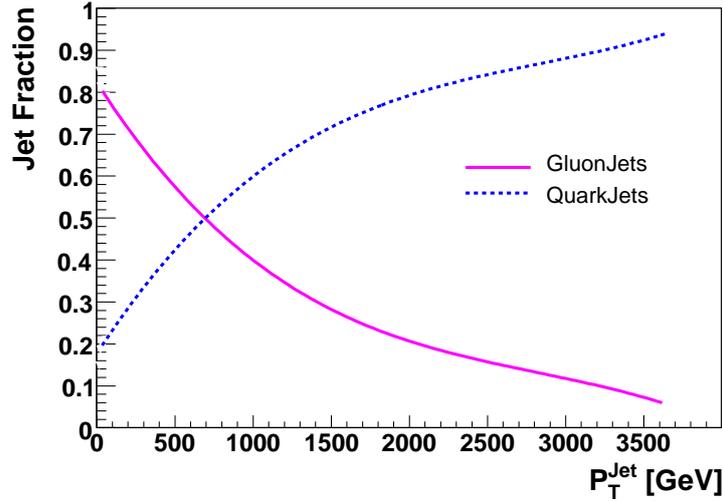


Figure 1: Fraction of the quark or gluon initiated jets as a function of jet  $p_T$  for  $|y| < 1$  (from PYTHIA DWT).

## 51 2 Definition of Jet Shapes

The jet shape is defined as the average fraction of the jet transverse momentum within a cone of a given size  $r$  around the jet axis,  $r = \sqrt{(y_i - y_j)^2 + (\phi_i - \phi_j)^2}$ , where  $i$  refers to the particle, calorimeter tower or track, and  $j$  to the jet. Jet shapes can be studied by using an integrated or a differential distribution. In the present study only two leading jets within  $|y| < 1$  are considered per event. All particles and calorimeter towers within distance  $R = \sqrt{(\Delta y)^2 + (\Delta \phi)^2} = 0.7$  from the jet axis are used. This large cone size ensures that most of the parent parton energy is included in the jet. The differential distribution,  $\rho(r)$ , is illustrated in Fig. 5. It is defined as the fraction of the jet transverse momentum contained inside an annulus of inner radius  $r - \delta r/2$  and outer radius  $r + \delta r/2$  around the jet axis, such that  $0 \leq r \leq R$ :

$$\rho(r) = \frac{1}{\delta r} \frac{1}{N_{jet}} \sum_{jets} \frac{p_T(r - \delta r/2, r + \delta r/2)}{p_T(0, R)}. \quad (1)$$

52 Above,  $N_{jet}$  denotes the total number of selected jets. In the numerator  $p_T$  is the sum of all  
 53 particles, tracks or towers in the distance range  $(r - \delta r/2, r + \delta r/2)$  from the jet axis. In the  
 54 denominator,  $p_T(0, R)$  is the scalar sum of transverse momenta of all the particles, tracks or  
 55 towers within the cone of radius  $R$ .

Similarly, the integrated jet shape (see Figure 6),  $\psi(r)$ , is defined as:

$$\psi(r) = \frac{1}{N_{jets}} \sum_{jets} \frac{p_T(0, r)}{p_T(0, R)} \quad (2)$$

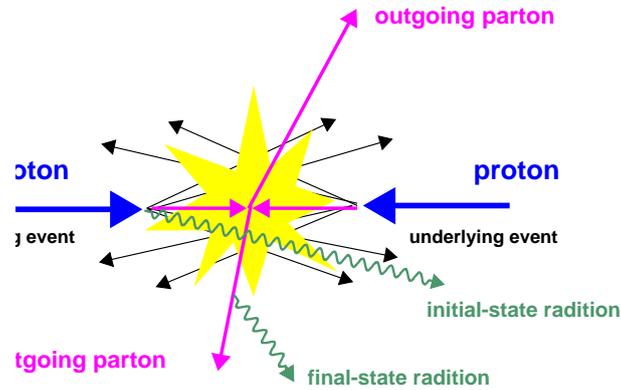


Figure 2: Illustration of a typical proton-proton two parton hard scattering event including initial and final state radiation and beam-beam remnants.

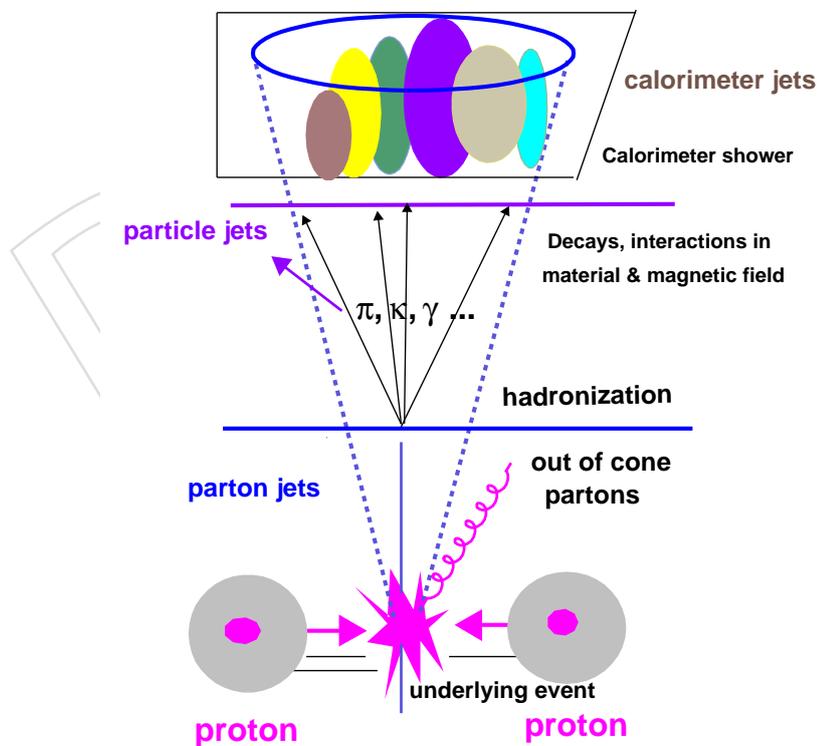


Figure 3: Schematic of jet evolution and detection. Parton jets hadronize into particle jets which interact in the calorimeter forming calorimeter jets.

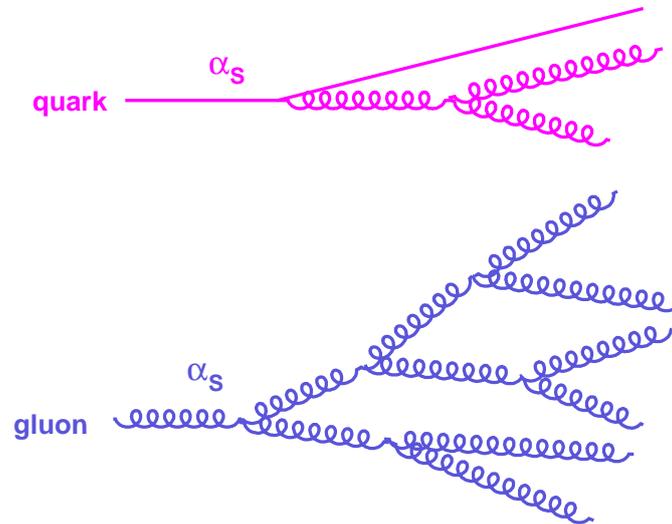


Figure 4: Examples of the structure of quark and gluon initiated jets

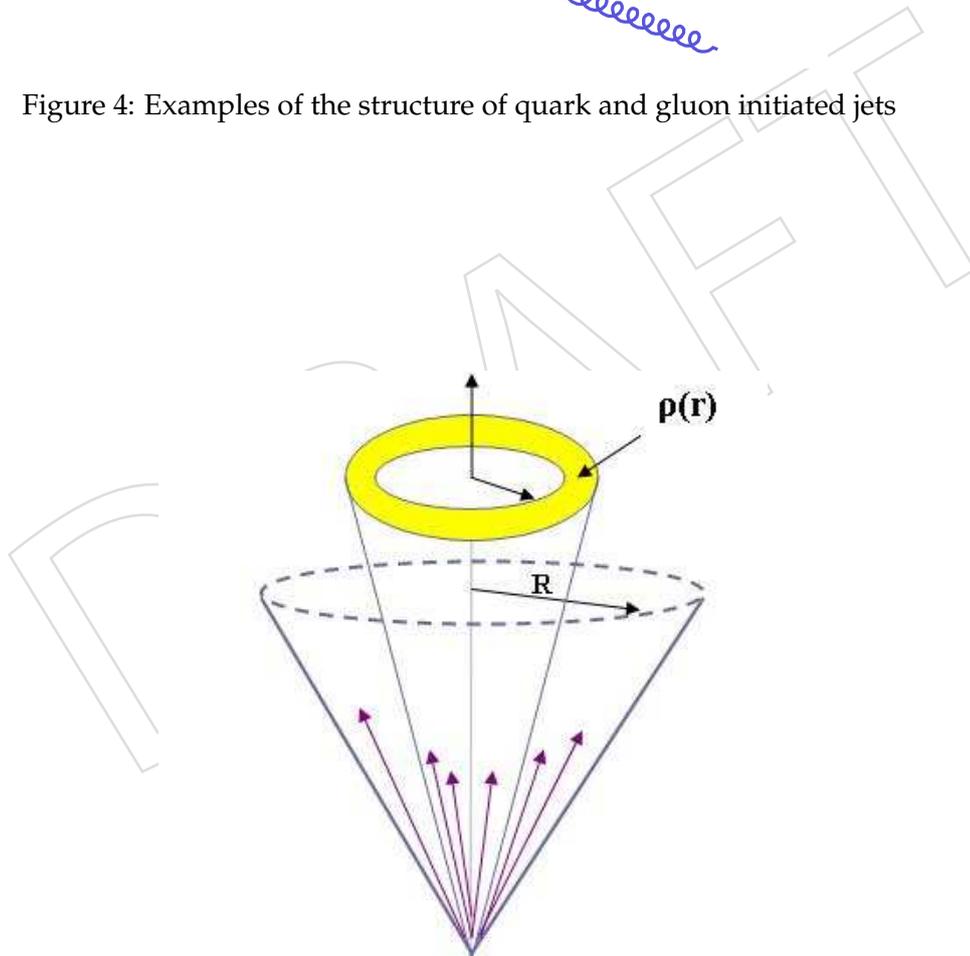


Figure 5: Definition of the differential jet shape,  $\rho(r)$ .

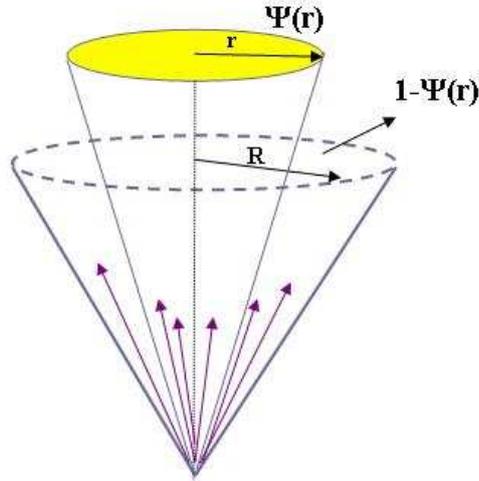


Figure 6: Definition of the integrated jet shape,  $\psi(r)$ .

56 where  $p_T(0, r)$  is the scalar sum of transverse momenta of all particles within the distance  $r$   
 57 from the jet axis with  $\psi(r = R) \equiv 1$ .

58 To calculate the jet shapes, we made histograms of transverse momentum in the appropriate  
 59 bin of  $r$  divided by the transverse momentum in the cone  $R = 0.7$ . The mean value of these  
 60 histograms was then plotted as function of  $r$ . The statistical uncertainty on each point was  
 61 calculated as  $rms/\sqrt{N}$ , using the  $rms$  of the corresponding histogram and the number  $N$  of  
 62 jets in the bin. For the integrated shape the uncertainties at different  $r$  points are partially  
 63 correlated.

### 64 3 CMS Detector

65 The Compact Muon Solenoid (CMS) detector is a multipurpose apparatus at the Large Hadron  
 66 Collider (LHC) at CERN. The CMS has a cylindrical structure covering almost  $4\pi$  of angular  
 67 phase-space in order to detect a large fraction of particles produced in a pp collision. It con-  
 68 tains subsystems which are designed to measure energies and momenta of photons, electrons,  
 69 muons, and hadrons [8–10].

70 The central hadronic section (HCAL) is made of brass and scintillators while the electromag-  
 71 netic section (ECAL) comprises lead tungstate crystals ( $PbWO_4$ ). The response of the calorime-  
 72 ter to photons is linear versus incident energy, while the response to hadrons depends strongly  
 73 on the incident energy. The difference in response of the calorimeter to photons and hadrons  
 74 leads to a nonlinear energy response of the calorimeter to jets.

75 The coordinate system used at CMS[11] is defined as follows: the  $x$ -axis points horizontally  
 76 outside the LHC ring, the  $y$ -axis points upwards, and the  $z$ -axis is aligned with the nominal  
 77 clock-wise beam direction. The azimuthal angle is  $\phi$  and the polar angle is  $\theta$ . The transverse  
 78 momentum  $p_T$  is defined as a projection of a particle momentum  $P$  on the  $xy$ -plane,  $p_T =$   
 79  $P \cdot \sin \theta$ , and the “transverse energy” as  $E_T = E \cdot \sin \theta$ . The rapidity is defined as  $y = \frac{1}{2} \log \frac{E+P_Z}{E-P_Z}$ ,  
 80 where  $E$  denotes the energy and  $P_Z$  is the component of the momentum along the  $z$  direction.  
 81 The pseudo-rapidity is defined as  $\eta = -\ln[\tan \frac{\theta}{2}]$ .

## 4 Jet Clustering Algorithms

In high energy interactions partons are produced in the final state with large transverse momenta as a result of the hard scattering process illustrated in Figure 2. Partons outgoing from the interaction point produce parton showers and subsequently partons from these showers combine to form hadrons which are color singlets which interact in the detector (see Figure 3). Since the transverse momenta involved in the hadronization process are much smaller than the hard scattering momenta, the final state particles are collimated around the direction of the original parton. These streams of particles are called jets. Jet clustering algorithms are used to associate particles to a particular jet. Direction and energy of a jet are related to the direction and energy of the original parton.

Many jet reconstruction algorithms are being used in CMS including iterative cone,  $k_T$ , SIS-Cone (Seedless Infrared Safe Cone) [12] and anti- $k_T$  algorithms [13]. The cone jet algorithm, such as SIS-Cone, groups the input objects together based on their distance in  $(y, \phi)$  space, and the determination of the jet quantities is done at the end of the jet finding. The successive recombination algorithms iteratively merge input objects into final jets and so the jet kinematic quantities, the jet direction and energy, are calculated directly during the clustering. In this analysis, the anti- $k_T$  algorithm has been used to reconstruct jets with  $D = 0.7$ . The anti- $k_T$  algorithm [13] starts with a list of proto-jets given by 4-momentum  $(E, p_x, p_y, p_z)$ . All the objects which are to be clustered are considered as proto-jets. The transverse momentum  $p_T$ , rapidity  $y$ , and azimuthal angle  $\phi$  of a proto-jet are calculated using give Equation 4.

$$(E, p_x, p_y, p_z) = \sum_i (E, p_x, p_y, p_z)_i \quad (3)$$

$$p_T = \sqrt{p_x^2 + p_y^2} \quad y_c = \frac{1}{2} \ln \left( \frac{E + p_z}{E - p_z} \right) \quad \phi_c = \tan^{-1}(p_y/p_x). \quad (4)$$

For each proto-jet  $i$  and the pair  $(i, j, i \neq j)$ ,  $d_i$  and  $d_{ij}$  are defined as

$$d_i = p_{T,i}^2 \quad d_{ij} = \min(p_{T,i}^{2p}, p_{T,j}^{2p}) \frac{(y_i - y_j)^2 + (\phi_i - \phi_j)^2}{D^2} \quad (5)$$

where  $D$  is the parameter which controls the size of the jet. For the anti- $k_T$  algorithm, the parameter  $p = -1$ . The algorithm determines the minimum  $d_{min}$  of the  $d_i$  and all the  $d_{ij}$ . If  $d_{min} = d_i$ , the proto-jet is not mergable and is promoted to a jet. Otherwise, the proto-jets  $i, j$  are merged into a single proto-jet with the 4-momentum  $(E_{ij}, \vec{p}_{ij}) = (E_i + E_j, \vec{p}_i + \vec{p}_j)$ . The process is repeated until no proto-jets are left. In anti- $k_T$  algorithm the measure  $d$  depends on the  $1/p_T^2$  of the object, clustering the high  $p_T$  objects first. This procedure leads to a circular jets.

## 5 Data sets and luminosity

### 5.1 Collider data

The data collected with minimum bias and jet triggers is used. Currently using Run 132601. and require that event pass bit 40 or bit 41. In addition, the event is required to be in-time with beam crossing by requiring the BPTX bit to be set. The lumi sections in range 261-1131 are used. The events which pass any of the Beam Halo triggers labeled by bits 36,37, 38, 39 are rejected. These halo rejection and timing requirements remove most of the non-physics background from the data. In addition, the ‘‘Monster events’’ were explicitly removed. These monster events are high track multiplicity events which are related with the beam but not with

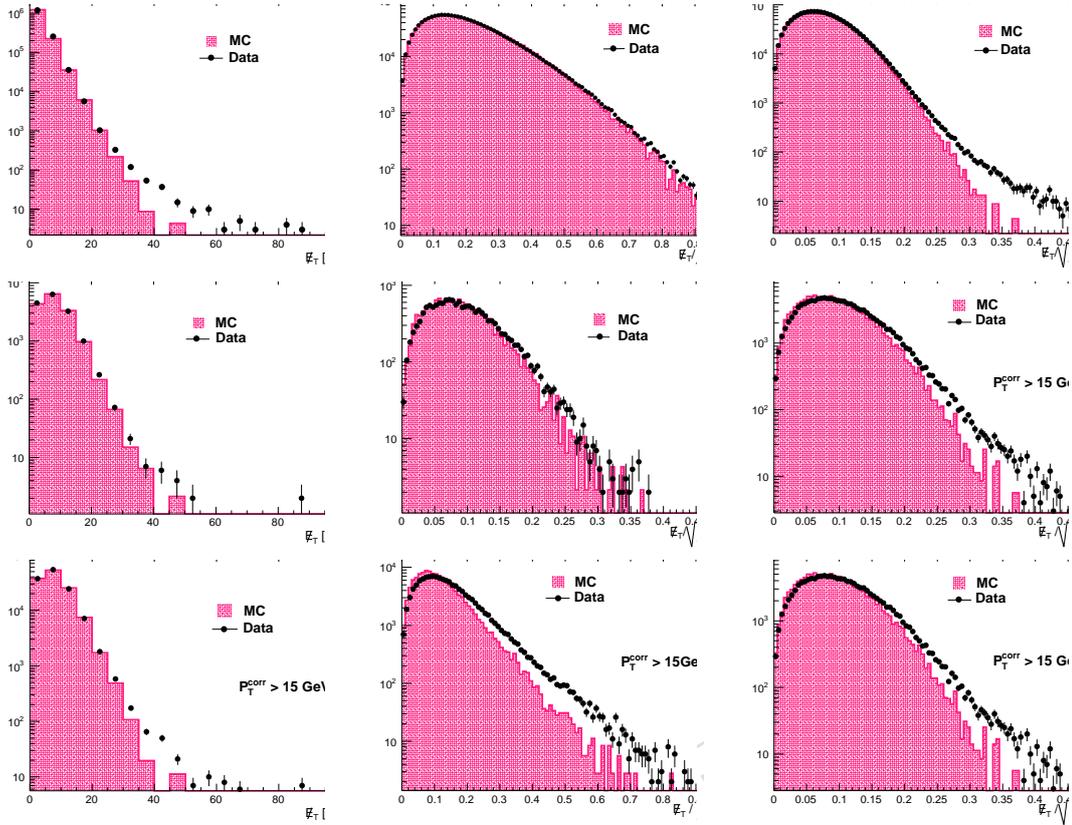


Figure 7:  $E_T$ ,  $E_T/\sum E_T$  and  $E_T$  significance  $E_T/\sqrt{\sum E_T}$  distributions in the data

107 the  $pp$  collisions close to the center of detector. Events were required to have at least one good  
 108 primary vertex vertex. The vertex selection cuts are given in Section 6.3.

109 The data sets used in this analysis are:

dataset	Name (RECO)	events	L
Data	/MinimumBias/Commissioning10-April-PromptReco-v8/		

## 111 5.2 Monte Carlo data

112 For QCD predictions we used PYTHIA event generator. Various data sets used are given below.

dataset	Name (GEN-SIM-RECO)	Cross section	Effective L
Pythia	/MinimumBias/Spring10-START3X.V26A.356ReReco-v1/		
Herwig	/MinimumBias/Spring10-START3X.V26A.356ReReco-v1/		

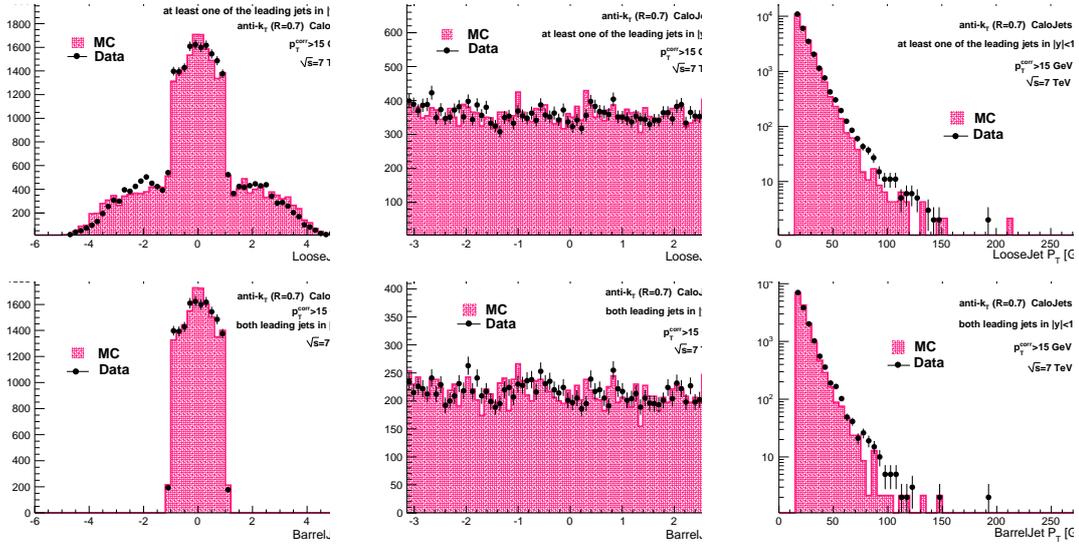
## 114 6 Analysis

### 115 6.1 Software

116 We use CMSSW version xxx.

### 117 6.2 Missing $E_T$ Significance

118 Figure 7 shows the distribution for  $E_T/\sum E_T$  in data compared to minimum bias data.

Figure 8:  $y$ ,  $\phi$  and  $p_T$  distributions of the selected jets.

### 6.3 Vertex Selection Criteria

We follow the CMS recommendations and use following cuts

Number of degrees of freedom	$\text{ndof} > 5$
$z$ position of the vertex	$ z  < 15 \text{ cm}$
Radial position of the vertex	$\sqrt{x^2 + y^2} < 2 \text{ cm}$

### 6.4 Jet Quality Requirements (Loose JetID)

Energy fraction observed in EM calorimeter	$\text{emf} > 0.01$ if the $ \eta^{\text{jet}}  < 2.6$
Number of hits containing $\geq 90\%$ of the jet energy	$\text{n90Hits} > 2$
Fraction of the jet energy contained in a single HPD	$\text{fHPD} < 0.98$

### 6.5 Track Selection

We use For tracking study we use high quality tracks. In addition we require that reach track has at least six valid hits ( $\text{nValidHits} \geq 6$ ). We use track with  $p_T \geq 0.3 \text{ GeV}$ .

High purity tracks	Yes
$p_T$	$\geq 0.3 \text{ GeV}$
$\text{nValidHits}$	$\geq 6$
$\sigma(p_T)/p_T$	$\leq 5$ (need to add)
$(z - z_{\text{vertex}})/\sigma(z - z_{\text{vertex}})$	$\leq 5$ (need to add)
$(d - d_{\text{vertex}})/\sigma\Delta_d$	$\leq 5$ (need to add)

### 6.6 Towers Selection

To calculate the jetshapes, we used calorimeter towers with  $p_T > 0.3 \text{ GeV}$ . The towers are constructed from electromagnetic calorimeter cells (crystals) and hadron calorimeter cells using Scheme 6 thresholds. In this scheme hadron calorimeter cell with energy  $> 0.xx \text{ GeV}$  are included. For EM calorimeter crystals, each crystal is required to have energy above  $0.090 \text{ GeV}$  and sum of 25 crystals contributing to a tower must be above  $0.2 \text{ GeV}$ . The ECAL crystals

Figure 9: Number of towers, tracks in a jets as a function of jet  $p_T$ .

134 are readout using a selective readout scheme i.e. all Crystal in 5x5 region around a cell of inter-  
135 est are readout without any zero-suppression threshold. If there is no cell of interest, only the  
136 cell with  $p_T > 1000$  GeV are readout.

## 137 **7 Multiplicity of Jet Constituents**

138 Figure 9 summarizes the mean multiplicities of particles, tracks and calorimeter towers in a jet  
139 as a function of jet  $p_T$ . As expected, they increase logarithmically with increasing jet  $p_T$ . Fig-  
140 ures 12, 10 and 11 present the multiplicity distributions for particles, calorimeter towers and  
141 tracks in a jet, respectively, in selected  $p_T$  bins. The data are compared with the MC predictions  
142 and shows a good agreement.

## 143 **8 $p_T$ Distributions of Particles, Tracks and Towers in a Jet**

144  $p_T$  distributions of particles, tracks and towers in a jet are shown in Figures 13, 15 and 14,  
145 respectively. These distributions become harder with increasing jet  $p_T$ .

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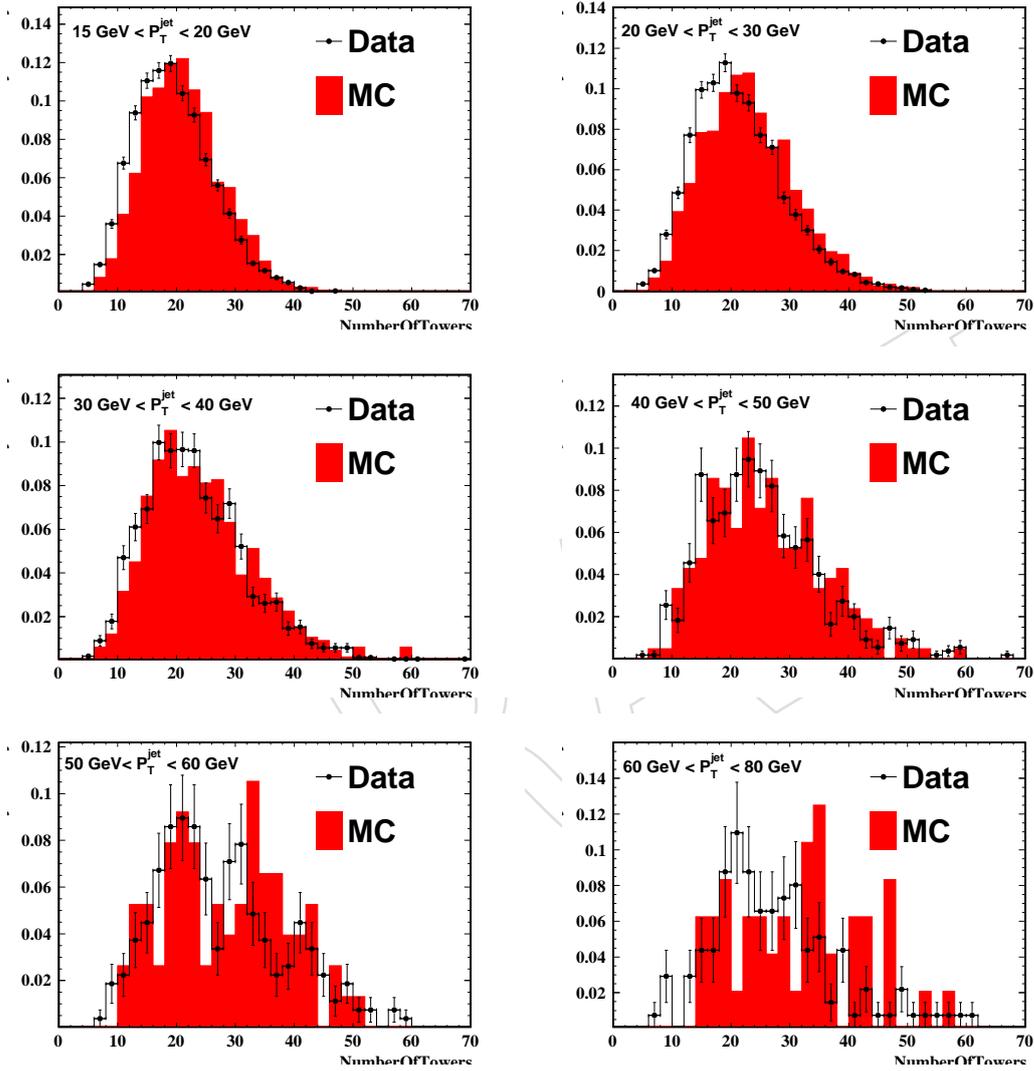


Figure 10: Number of towers with  $R = 0.7$  of the jet axis in bins of  $p_T$  of the jet in CMS data at  $\sqrt{s} = 7$

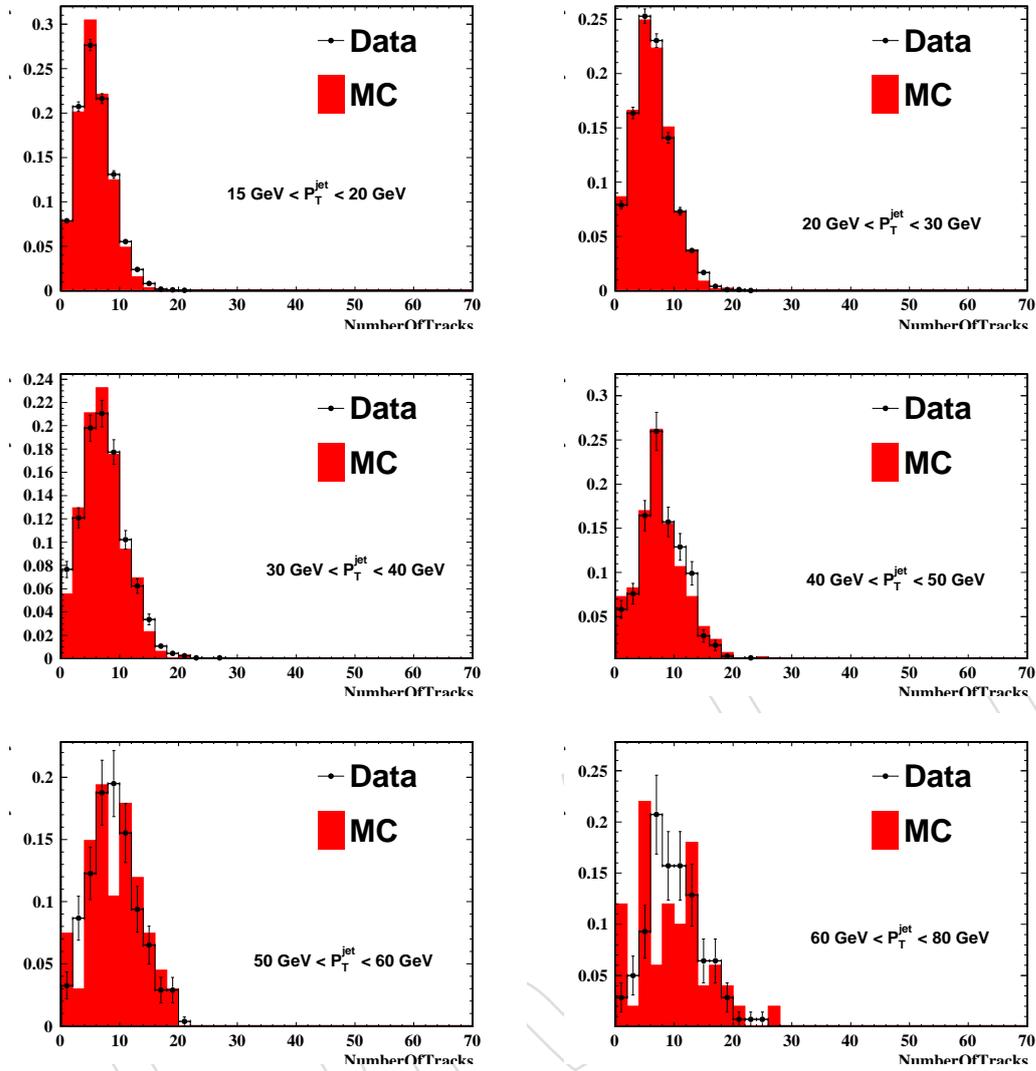


Figure 11: Number of good tracks with  $R = 0.7$  of the jet axis in bins of  $p_T$  of the jet in CMS data at  $\sqrt{s} = 7$

Figure 12: Number of particles with  $R = 0.7$  of the jet axis in bins of  $p_T$  of the jet in PYTHIA MC QCD multijet events

Figure 13: The  $p_T$  distribution of the stable particles in a jet for different jet  $p_T$  bins in PYTHIA Monte Carlo events.

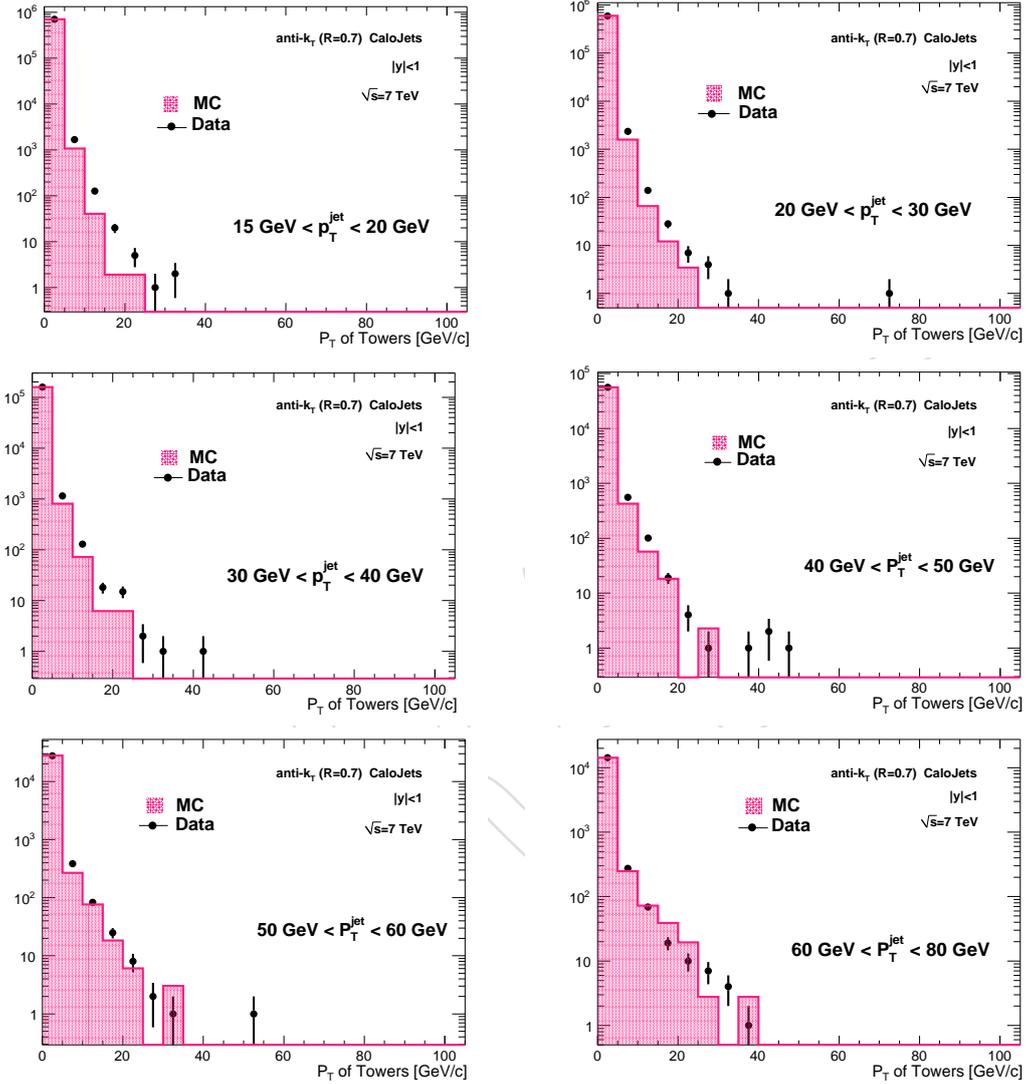


Figure 14: The  $p_T$  distribution of the towers in a jet for different jet  $p_T$  bins. The data are compared to the MC predictions.

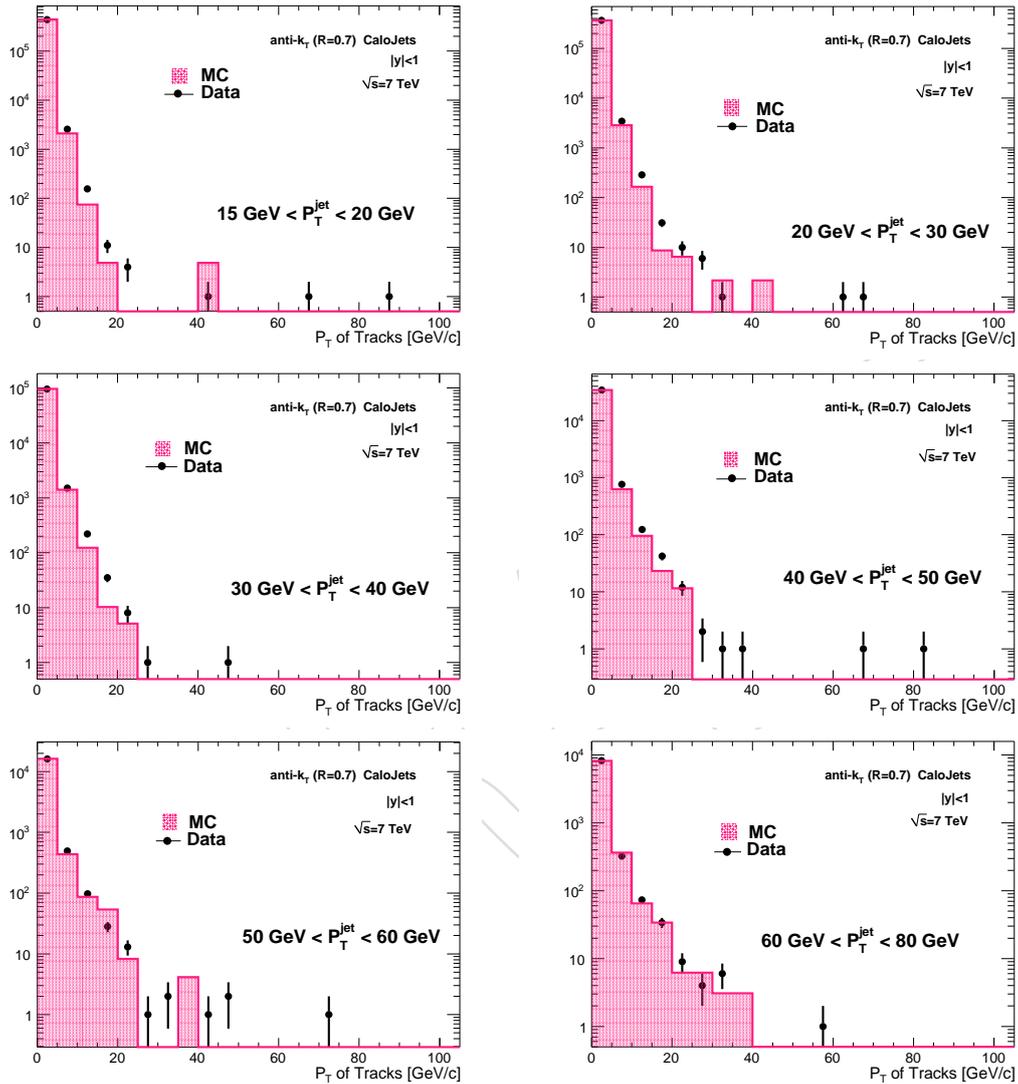


Figure 15: The  $p_T$  distribution of the tracks in a jet for different jet  $p_T$  bins. The data are compared to the MC predictions.

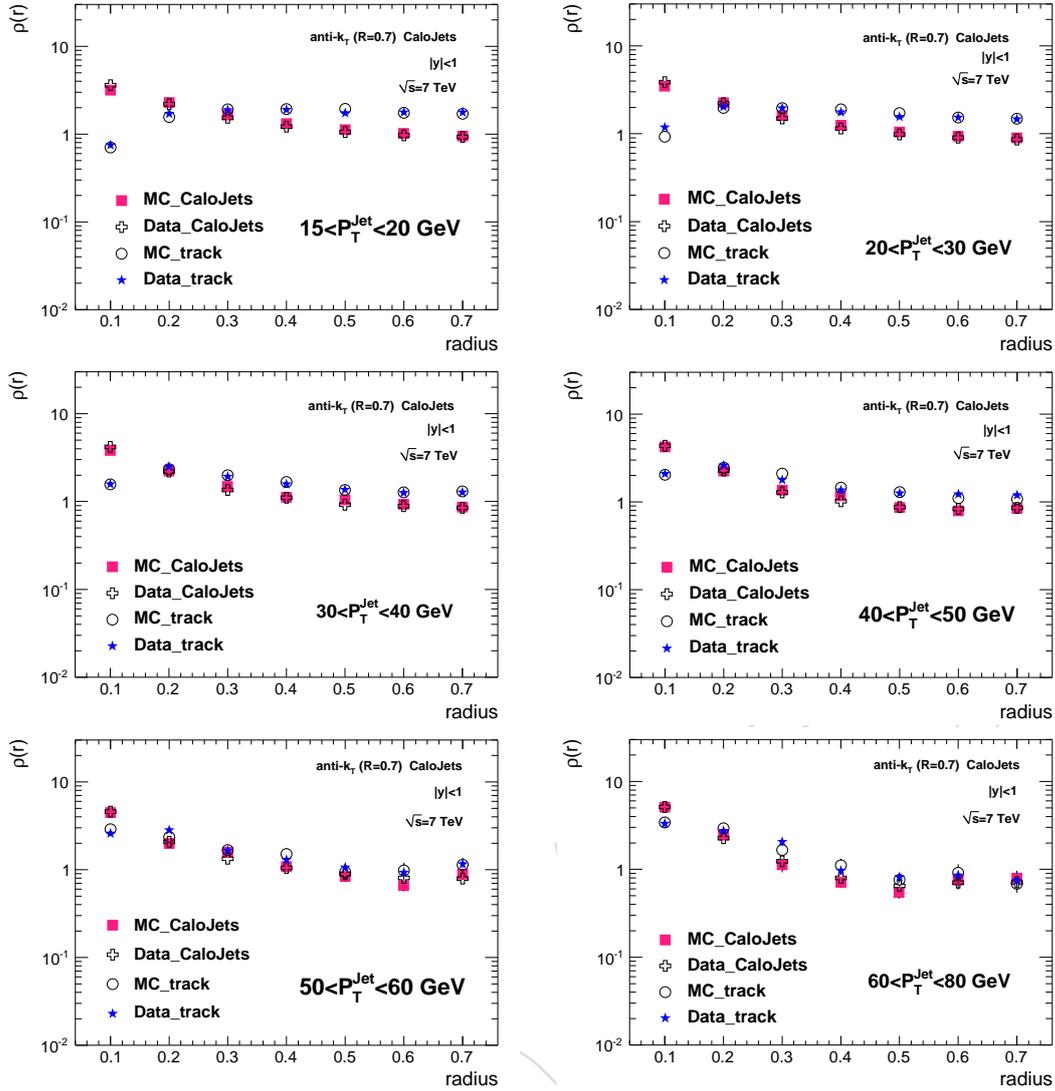


Figure 16: Differential jetshpes for jet in various  $p_T^{\text{Jet}}$  bins. The data are compared with PYTHIA predictions for both calorimeter jetshpes and track jetshpes.

## 146 9 Raw Jet Shapes

147 Figure 16 and Figure 17 show the differential and integrated jet shapes for data events measured using calorimeter towers for various jet  $p_T$  bins. Most of the momentum is concentrated  
 148 within a small region around the jet axis. Jet shapes become narrower with the increasing  $p_T$   
 149 of the jet. The data are in good agreement with the calorimeter jetshpes predicted by PYTHIA  
 150 event generator using underlying event tune DW. The jetshpes measured using tracks is also  
 151 shown for both data and simulated events and show good agreement. The jetshpes measured  
 152 using tracks also show the the same trend, though they are slightly wider.  
 153

## 154 10 Jet Shape Corrections

155 Due to various detector effects, the measured (calorimeter) jet shapes are different than the true  
 156 (particle) jet shapes. Due to the magnetic field of CMS, charged particles with  $p_T < 0.9$  GeV

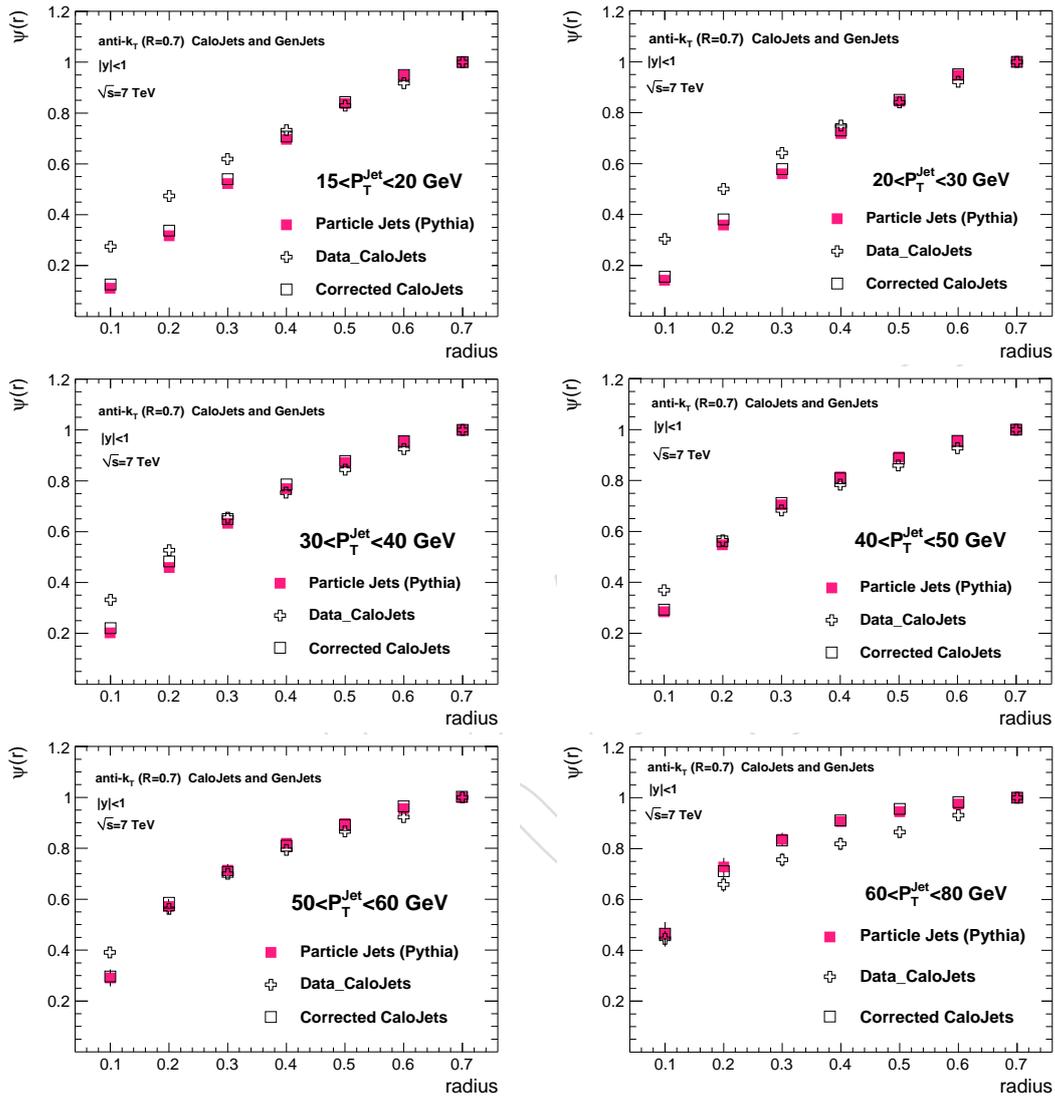


Figure 17: Integrated jetshpes for jet in various  $p_T^{\text{jet}}$  bins. The data are compared with PYTHIA predictions for both calorimeter jetshpes and track jetshpes.

Figure 18: Correction factors for differential jetshpes for jet in various  $p_T^{\text{Jet}}$  bins as determined from PYTHIA MC event generator.

Figure 19: Correction factors for integrated jetshpes for jet in various  $p_T^{\text{Jet}}$  bins as determined from PYTHIA MC event generator.

157 do not reach the calorimeter. In addition showers from particles interacting with the detector  
 158 material spread their energy over many calorimeter towers. The measured jet shapes must  
 159 be corrected for these detector effects. Correction factors were determined as a function of  
 160 distance from the jet axis using MC events before and after the CMS detector simulation. For  
 161 this approach to be valid, the MC simulation must describe the calorimeter response accurately.  
 162 Currents studies of the single particle response show that the data are well described by the  
 163 data [14]. The corrections have been determined using unmatched jets and are applied as a  
 164 function of distance from the jet axis.

165 The correction factors  $C_D(r)$  and  $C_I(r)$  for differential and integrated jet shapes are defined in  
 166 Equations 5 and 6, respectively:

$$C_D(r) = \rho_{MC}^{\text{PARTICLE}}(r) / \rho_{MC}^{\text{CAL}}(r) \quad (6)$$

$$C_I(r) = \psi_{MC}^{\text{PARTICLE}}(r) / \psi_{MC}^{\text{CAL}}(r) \quad (7)$$

167 where calorimeter towers and generated particles have been used to reconstruct differential  
 168  $\rho_{MC}^{\text{CAL}}(r)$ ,  $\rho_{MC}^{\text{PARTICLE}}(r)$  and integrated jet shapes  $\psi_{MC}^{\text{CAL}}(r)$ ,  $\psi_{MC}^{\text{PARTICLE}}(r)$  in different bins of jet  $p_T$ .

169 Measured calorimeter jet shapes are then used to determine the corrected differential jet shapes  
 170  $\rho^{\text{corrected}}(r) = C_D(r) \cdot \rho^{\text{CAL}}(r)$  and integrated jet shapes  $\psi^{\text{corrected}}(r) = C_I(r) \cdot \psi^{\text{CAL}}(r)$ .

171 The correction factors  $C_D(r)$  in Figure 18 do not show a significant dependence on jet  $p_T$  in  
 172 the region  $r < 0.5$ . They vary between 0.6 and 1.3 as a function of  $r$ , and between 1.3-2 for the  
 173 region  $r > 0.5$ . The correction factors for integrated jet shapes in Figure 19 vary from 0.9 to 1.06  
 174 for all radius and  $p_T$  bins. For the integrated distributions, the correction factors do not have a  
 175 strong dependence on jet  $p_T$ .

## 176 11 Corrected Jet Shapes

177 The corrected differential and integrated jet shapes are shown in Figures 20 and 21. Close to  
 178 the jet axis, the jet shape is dominated by collinear gluon emission, whereas at large distance  
 179 from the jet axis, the jet shape reflects large angle gluon emissions, which can be calculated  
 180 perturbatively. The jet shape  $\psi(r)$  increases faster with  $r$  for jets at larger  $p_T$  indicating that  
 181 these jets are more collimated.

## 182 12 Sensitivity of Jet Shapes to Underlying Event Tunes

183 The energy from the underlying event (UE) contributes to jets and impacts the jet shapes. To  
 184 determine the sensitivity of jet shapes to the UE contribution, event samples were generated

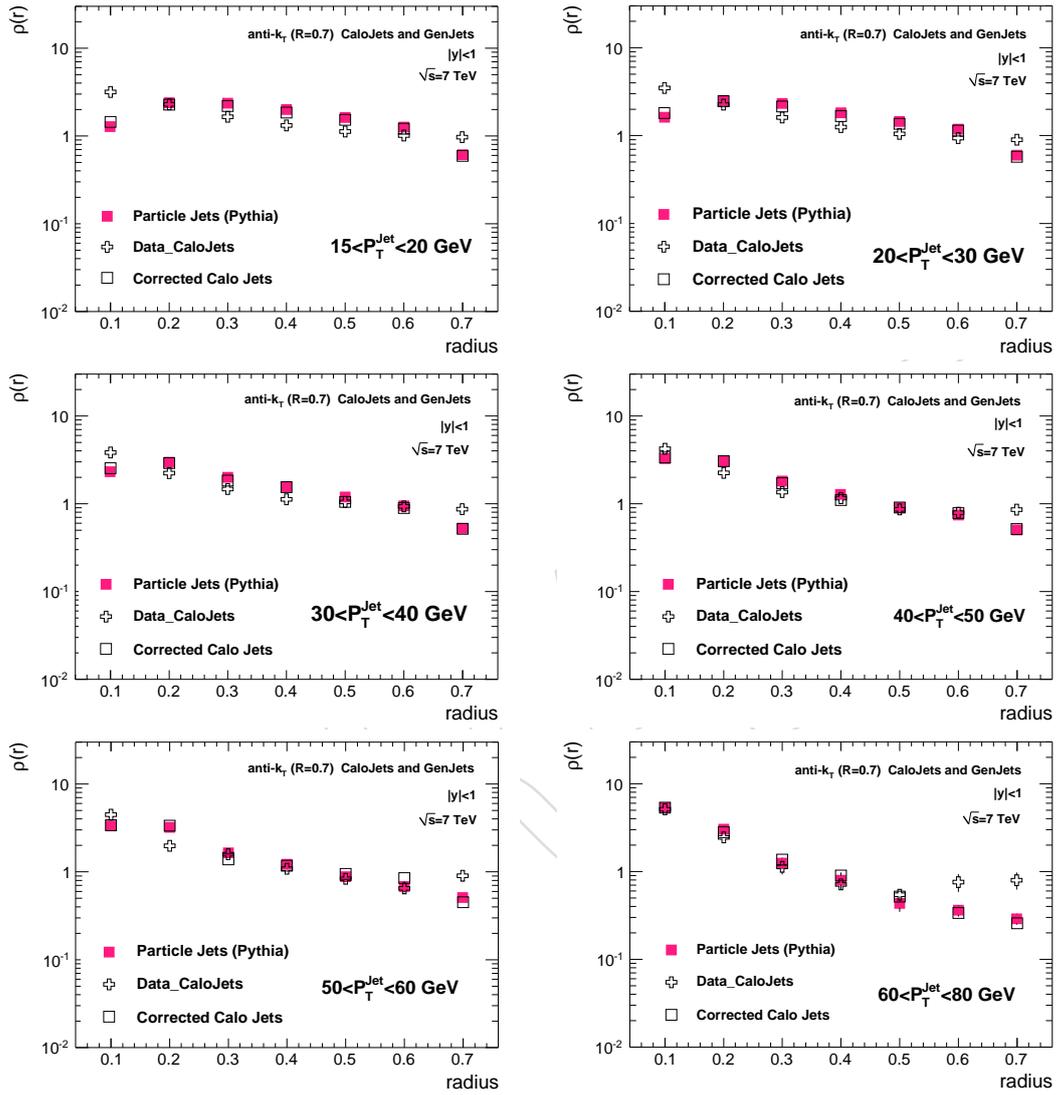


Figure 20: Particle level differential jetshpes for jet in various  $p_T^{\text{Jet}}$  bins. The data are compared with PYTHIA predictions.

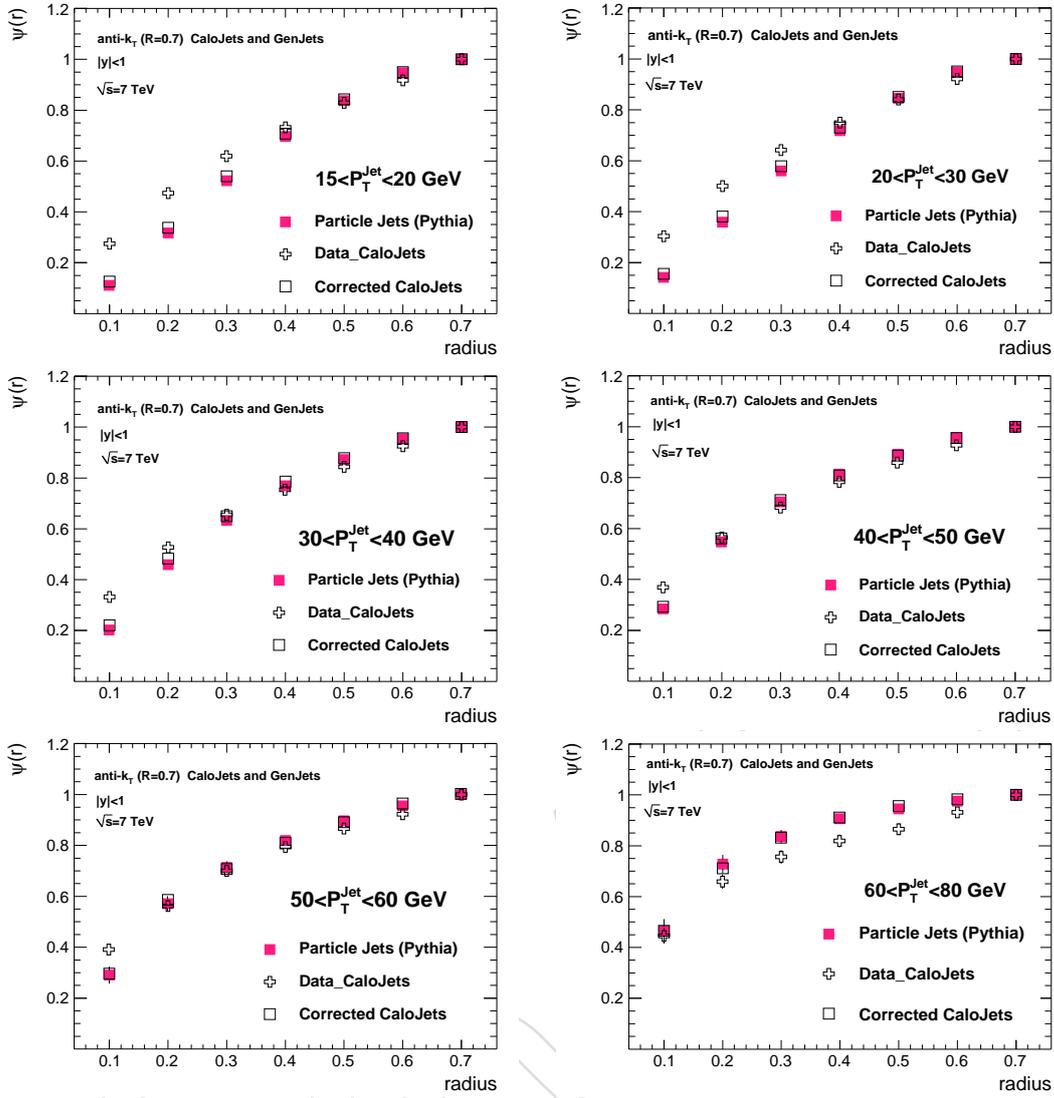


Figure 21: Particle level integrated jetshpes for jet in various  $p_T^{\text{Jet}}$  bins. The data are compared with PYTHIA predictions.

Figure 22: Differential jetshpes for jet in various  $p_T^{\text{Jet}}$  bins compared to PYTHIA MC predictions using different UE tunes

Figure 23: Integrated jetshpes for jet in various  $p_T^{\text{Jet}}$  bins compared to PYTHIA MC predictions using different UE tunes

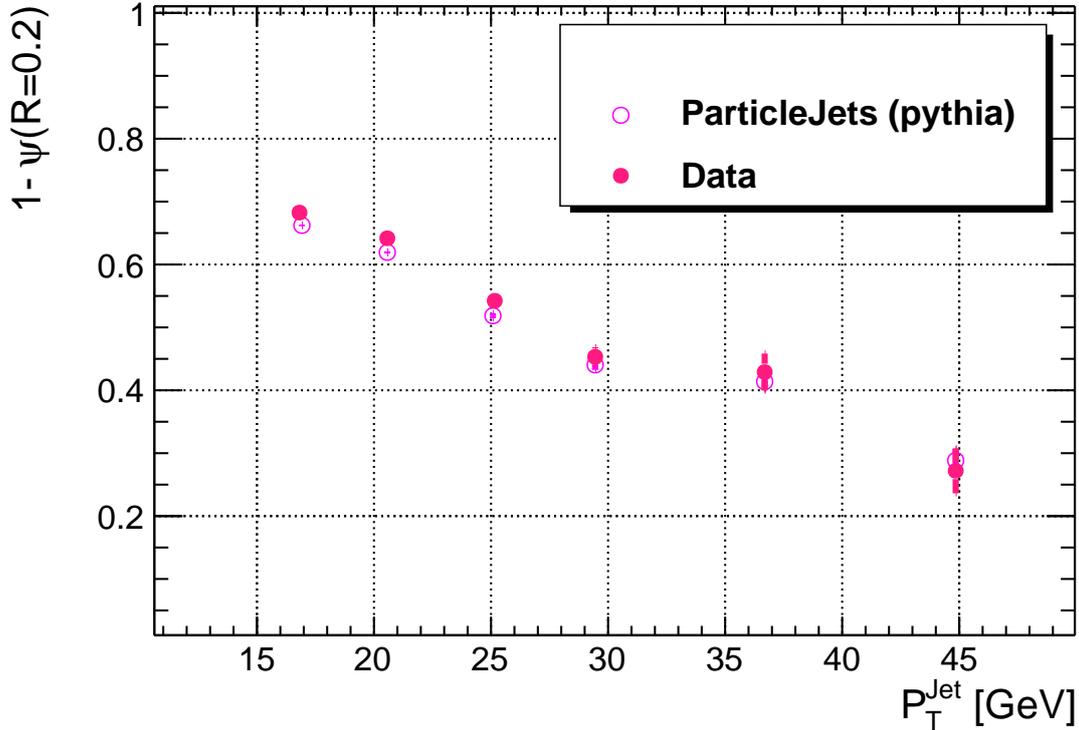


Figure 24: Jet transverse momentum fraction outside  $r=0.2$  regions.

185 using PYTHIA DW which has a smaller UE contribution than PYTHIA with tune DWT, which  
 186 is the CMS default setting [15]. These tunes are different extrapolations to  $\sqrt{s}=7$  TeV of the  
 187 same tune at the Tevatron energy  $\sqrt{s}=1.8$  TeV. The jet shapes for PYTHIA DWT and PYTHIA  
 188 DW are shown in Fig. 22 for the differential jet shapes and in Figure 23 for the integrated jet  
 189 shapes. At low jet  $p_T$ , one can observe the difference in jet shapes due to the UE contribution.  
 190 Underlying event contribution as a fraction of the jet  $p_T$  is larger at low  $p_T$  and at large radii.

### 191 13 Quark and Gluon Jet Shapes

192 Jet shapes are sensitive to quark and gluon jet contributions. The quark jets are narrower than  
 193 the gluon jets due to the coupling strengths for gluon emission which depend on the color  
 194 factors  $C_F=4/3$  for radiating quarks and  $C_A=3$  for gluons. It is instructive to separate the jets by  
 195 the flavor and study their shapes. As shown above in Fig 1, the flavor composition of the jets  
 196 in QCD multi-jet sample changes with the transverse energy of the jets as the proton parton  
 197 distribution change with momentum fraction  $x$ . Fraction of jet momentum with  $r \leq 0.2$  is  
 198 shown in Fig. 24. The data are compared with parton shower+hadronization MC predictions  
 199 for quark and gluon jets. Tables 2, 3 and 4 provide details of the calculation of statistical and  
 200 systematic uncertainties for  $1 - \psi(r = 0.2)$  in all  $p_T$  bins. The simulated jets are classified as  
 201 quark or gluon jets by matching the particle jets with a parton from  $2 \rightarrow 2$  scattering within  
 202  $\Delta R < 0.5$  in  $(y, \phi)$  space. The MC predicts that the measured jet shapes are dominated by  
 203 contributions from gluon initiated jets at low jet  $p_T$  while contributions from quark initiated jets  
 204 become important at high jet  $p_T$ . MC also predicts that the both quark and gluon jets become  
 205 narrower with increasing jet  $p_T$ . The data are in qualitative agreement with these predictions.

## 14 Systematic Uncertainties

The main sources of systematic uncertainties include:

- Jet energy scale
- Transverse shape of calorimeter showers
- Non-linearity of calorimeter response
- Jet fragmentation

The uncertainties arising from jet energy and position resolution, and from event selection cuts are expected to be negligible compared to the sources listed above and are not considered.

### 14.1 Jet Energy Scale

Current expectation of the JES uncertainty at start up is  $\pm 10\%$  [16]. Changing the JES correction within its uncertainty changes the jet shapes as jets migrate between  $p_T$  bins. Jet shapes vary slowly with jet  $p_T$  and thus this effect is expected to be small. To determine the impact on the jet shapes, we changed the  $p_T$  of the jet by  $\pm 10\%$  and repeated the whole analysis. The comparison between the default JES corrections and the modified corrections is shown in Figure 25. The corresponding systematic uncertainties on the differential jet shape are 10% at  $r=0.1$  and  $< 5\%$  at  $r = 0.2$  for all jet  $p_T$ . At larger  $r \geq 0.5$  they are  $< 20\%$ .

The uncertainties on the integrated jet shape are 10% at  $r=0.1$ , 5% at  $r=0.2$  for  $p_T < 100$  GeV, and decrease as a function of  $r$ . They are  $< 2\%$  at  $r=0.1$  for  $p_T > 100$  GeV and negligible at  $r > 0.1$ , as shown in Figure 26. The systematic uncertainty at  $r=0.7$  is 0 by definition of the integrated jet shape.

### 14.2 Jet Fragmentation

Because the calorimeter response depends on the momenta of the particles in the jets, modeling of jet fragmentation contributes to the uncertainty on the corrected jet shapes. Uncertainties due to the fragmentation model can be estimated by comparing the correction factors determined using PYTHIA and HERWIG events. The model of the underlying event used in HERWIG++ is described in [17]. Particle level differential and integrated jet shapes in PYTHIA DWT and HERWIG++ 2.2 [18] are shown in Figure 27 and Figure 28. Their observed difference is less than 5% at  $r < 0.3$ . To determine the systematic uncertainty due to modeling of jet fragmentation we compared PYTHIA DWT and HERWIG++ differential jet shape correction factors, shown in Figure 29. They agree to  $< 10\%$  for  $r \leq 0.2$ , however, the differences can be as large as 30 – 40% at  $r \geq 0.5$ . Note that the jet energy fraction at large  $r$  is small, which makes uncertainties on the differential jet shape measurement large in this region.

Comparisons of the integrated jet shape correction factors for PYTHIA DWT and HERWIG++ are shown in Figure 30. They agree within 5% (2%) at  $r=0.1$  (0.2) for  $60 < p_T < 80$  GeV. For  $p_T > 80$  GeV the differences range between 5 – 10% at  $r=0.1$  and are less than 5% at  $r=0.2$ . These differences decrease with increasing radius  $r$  for all jet  $p_T$ .

The correction factors have been also compared for PYTHIA DWT and PYTHIA DW simulations. The differences are less than 20% at  $r=0.1$  and  $< 10\%$  at  $r = 0.2$ . For differential jet shapes at large  $r$ , they can be as large as 20 – 30%. For integrated jet shapes, they become smaller for the high  $p_T$  jets and decrease with increasing  $r$ . The comparisons of correction factors for PYTHIA DWT and PYTHIA DW are shown in Figure 31 for differential jet shapes and in Figure 32 for integrated jet shapes.

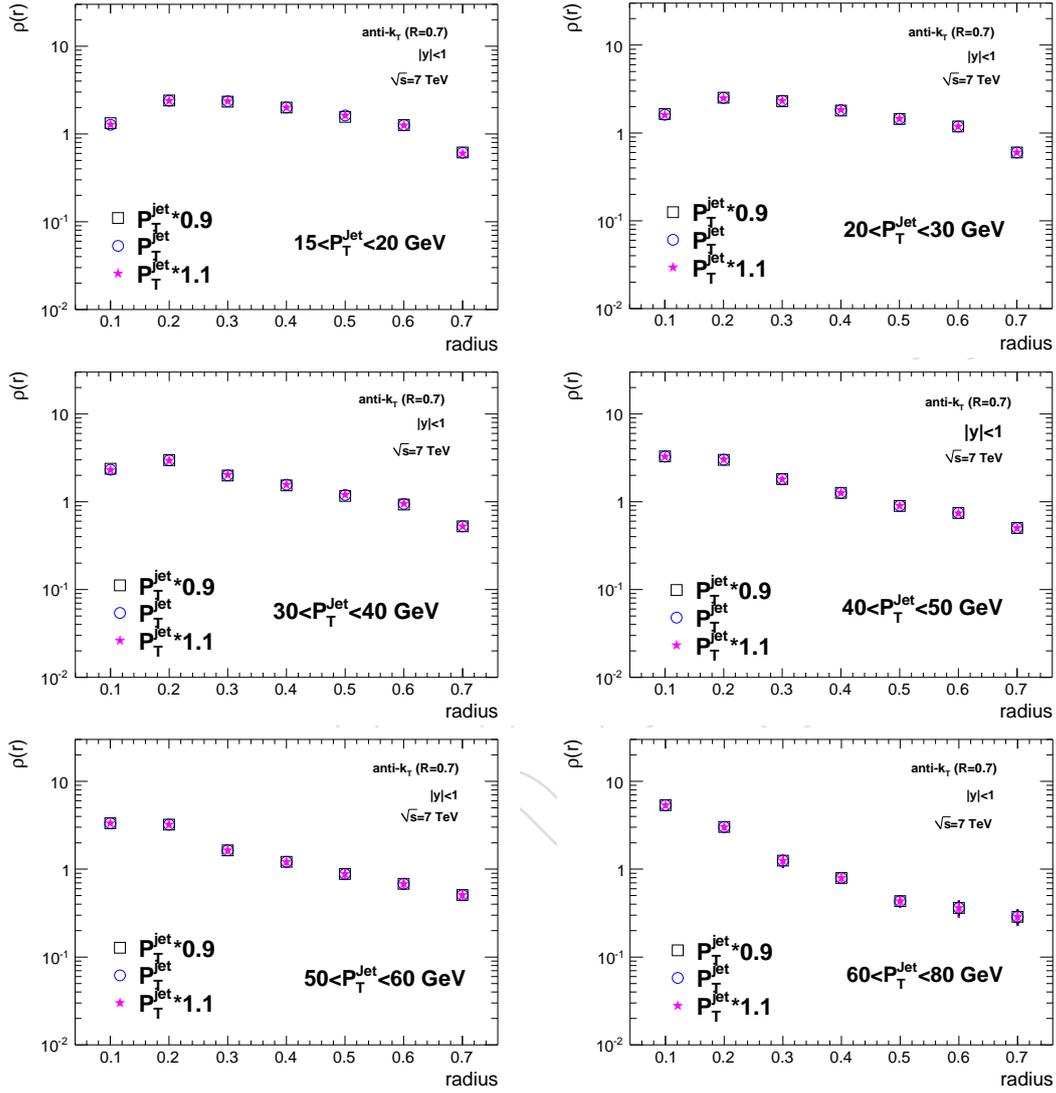


Figure 25: The fractional change in the differential jetshapes due to uncertainty in the jet energy scale determined by changing the jet energy scale by  $\pm 10\%$  independent of jet  $p_T$  and  $y$ .

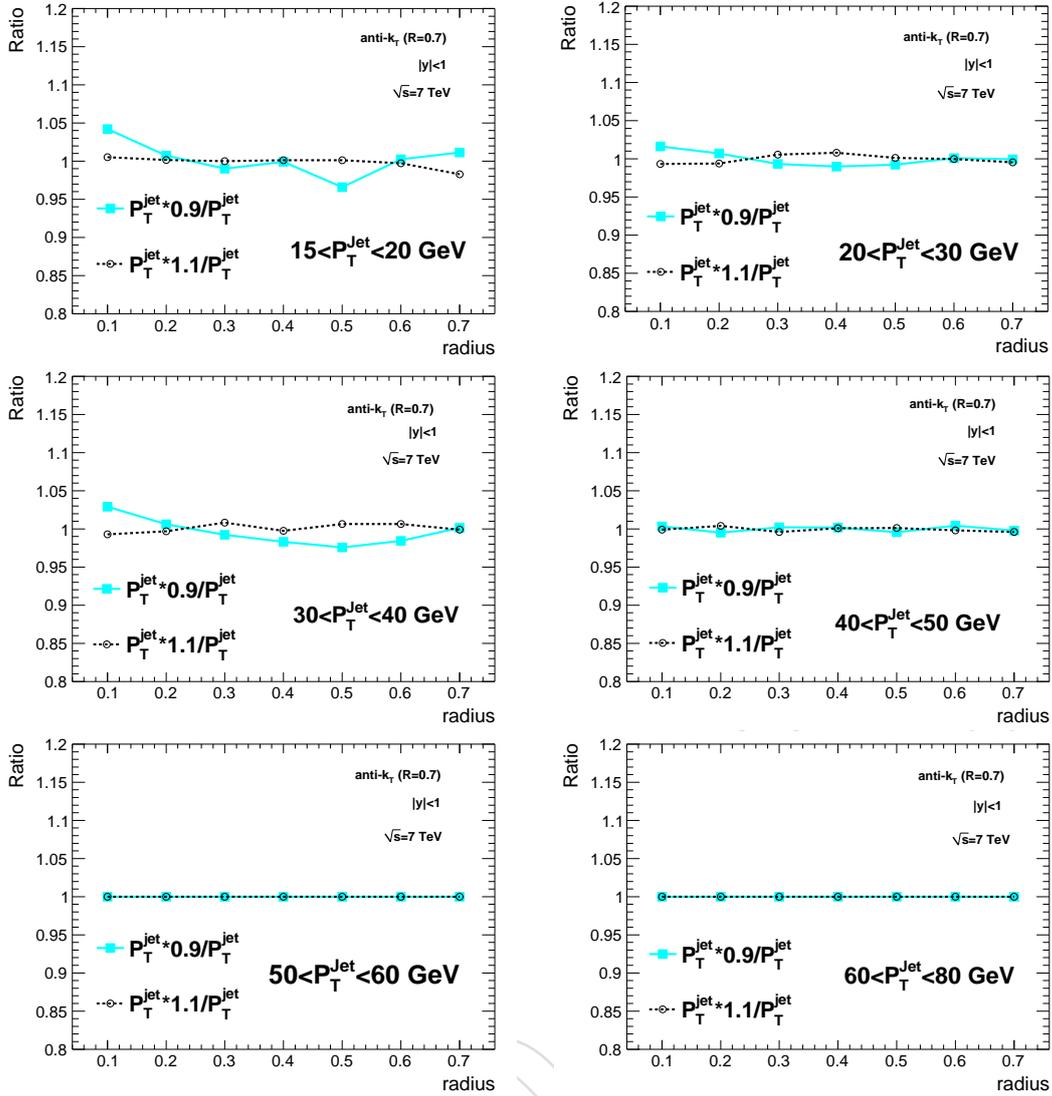


Figure 26: The fractional change in the integrated jetshapes due to uncertainty in the jet energy scale determined by changing the jet energy scale by  $\pm 10\%$  independent of jet  $p_T$  and  $y$ .

Figure 27: Particle level differential jetshapes as predicted by PYTHIA and HERWIG event generators for selected  $p_T^{\text{Jet}}$  bins.

Figure 28: Particle level integral jetshapes as predicted by PYTHIA and HERWIG event generators for selected  $p_T^{\text{Jet}}$  bins.

Figure 29: Corrections factor for differential jetshapes as determined from PYTHIA and HERWIG event generators for selected  $p_T^{\text{Jet}}$  bins.

Figure 30: Corrections factor for differential jetshapes as determined from PYTHIA and HERWIG event generators for selected  $p_T^{\text{Jet}}$  bins.

Figure 31: Corrections factor for differential jetshapes determined using two different tunes of the PYTHIA event generator for selected  $p_T^{\text{Jet}}$  bins.

### 14.3 Non-linearity of Calorimeter Response and Transverse Shower Profile

The uncertainties due to CMS calorimeter simulation can be estimated by comparing track jet shapes with calorimeter jet shapes in simulated and collider data. Here we assume that track reconstruction inefficiency and fake rate are small in both data and MC and have negligible effect on track jet shapes. In addition, it is assumed that any difference in calorimeter response to photons in data and MC is much smaller than possible difference in calorimeter response to hadrons. The track jetshapes are compared to calorimeter jetshapes in Figure ?? for data and the PYTHIA predictions. These ratios, under above assumptions, show the effective calorimeter response to particles as a function of  $r$ . The two responses are very close. The difference is assigned as the systematic uncertainty on the observed jetshapes.

As shown in Fig' 33, the scale factor  $SF$  as defined below is very close to 1.0 showing that calorimeter simulation describes the observed calorimeter response very well. The difference from unity is assigned as systematic uncertainty. and the deviation from unity is assigned as the systematic uncertainty. At large  $r$ , the particles are very soft. Some of the particles do not reach the calorimeter. The calorimeter response to the particles which do reach the calorimeter is low. Thus the ratio of calo-jetshapes to track-jetshape is large. Analogous procedure is used for the integrated jet shapes (see Fig. 34.)

$$SF = \frac{R^{DATA}}{R^{MC}} \quad \text{where} \quad R^{MC} = \frac{\text{TrackJetShape}}{\text{CaloJetShape}} \Big|_{MC}, \quad R^{DATA} = \frac{\text{TrackJetShape}}{\text{CaloJetShape}} \Big|_{DATA} \quad (8)$$

## 15 Conclusions

We have measured differential and integrates jetshapes of the jets with  $15 < p_T < 150$  GeV in  $|y| < 1.0$  region produced in  $pp$  collisions at  $\sqrt{s} = 7$  TeV. These jets become narrower with increasing jet transverse momentum, in good agreement with QCD inspired event generators, PYTHIA and HERWIG. The observed jetshapes are closer to gluon jetshapes at low  $p_T$  and tend toward quark jetshapes at high  $p_T$ . A comparison of these jetshapes with different PYTHIA tunes shows that these data prefer CW tune.

Several sources of systematic uncertainties were investigated, arising from jet energy calibration, jet fragmentation, calorimeter response and transverse showering, as function of jet  $p_T$  and distance from jet axis  $r$ . The systematic uncertainty is dominated by overall jet energy

Figure 32: Corrections factor for integral jetshapes determined using two different tunes of the PYTHIA event generator for selected  $p_T^{\text{Jet}}$  bins.

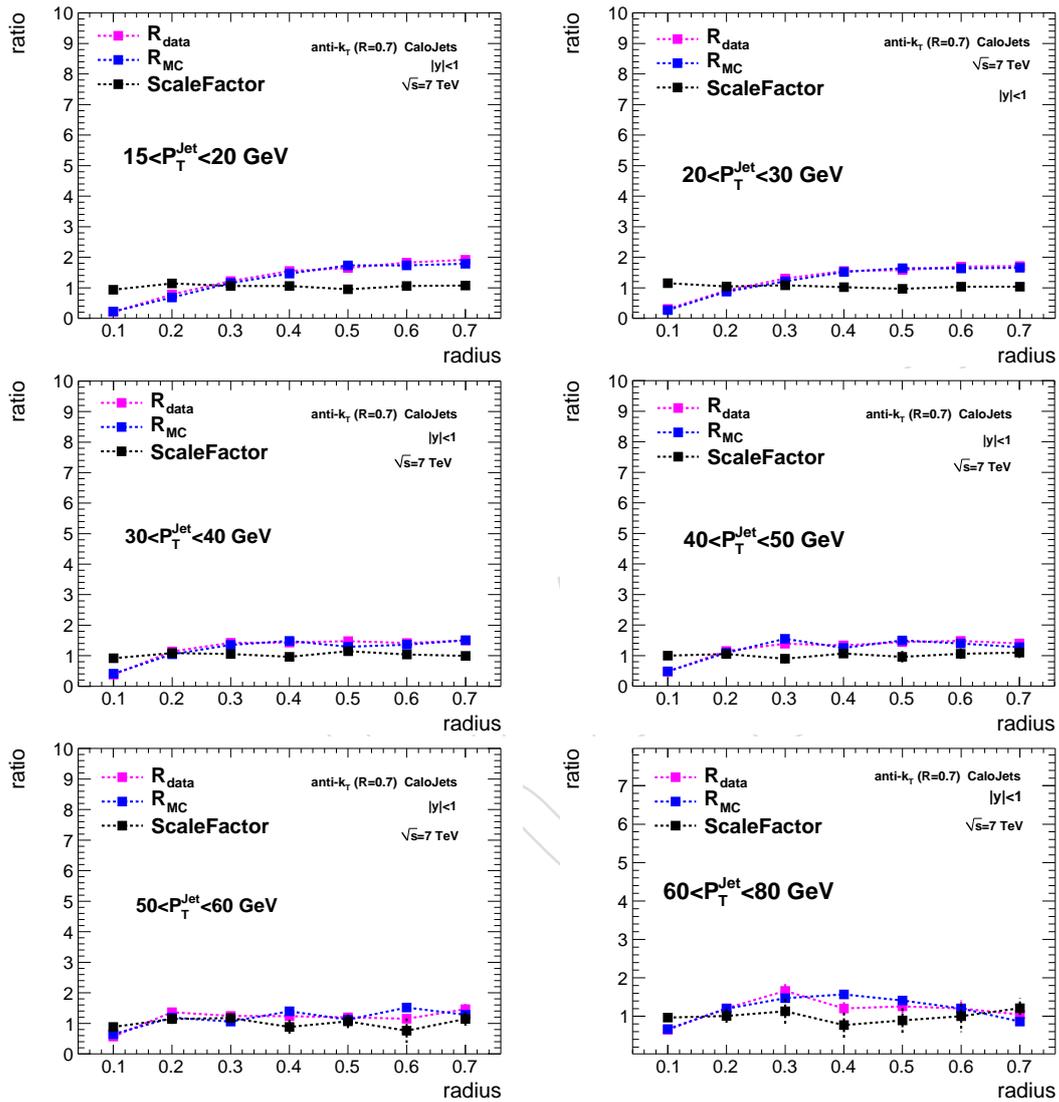


Figure 33: The fractional change in the differential jetshapes due to uncertainty in the jet energy scale determined by changing the jet energy scale by  $\pm 10\%$  independent of jet  $p_T$  and  $y$ .

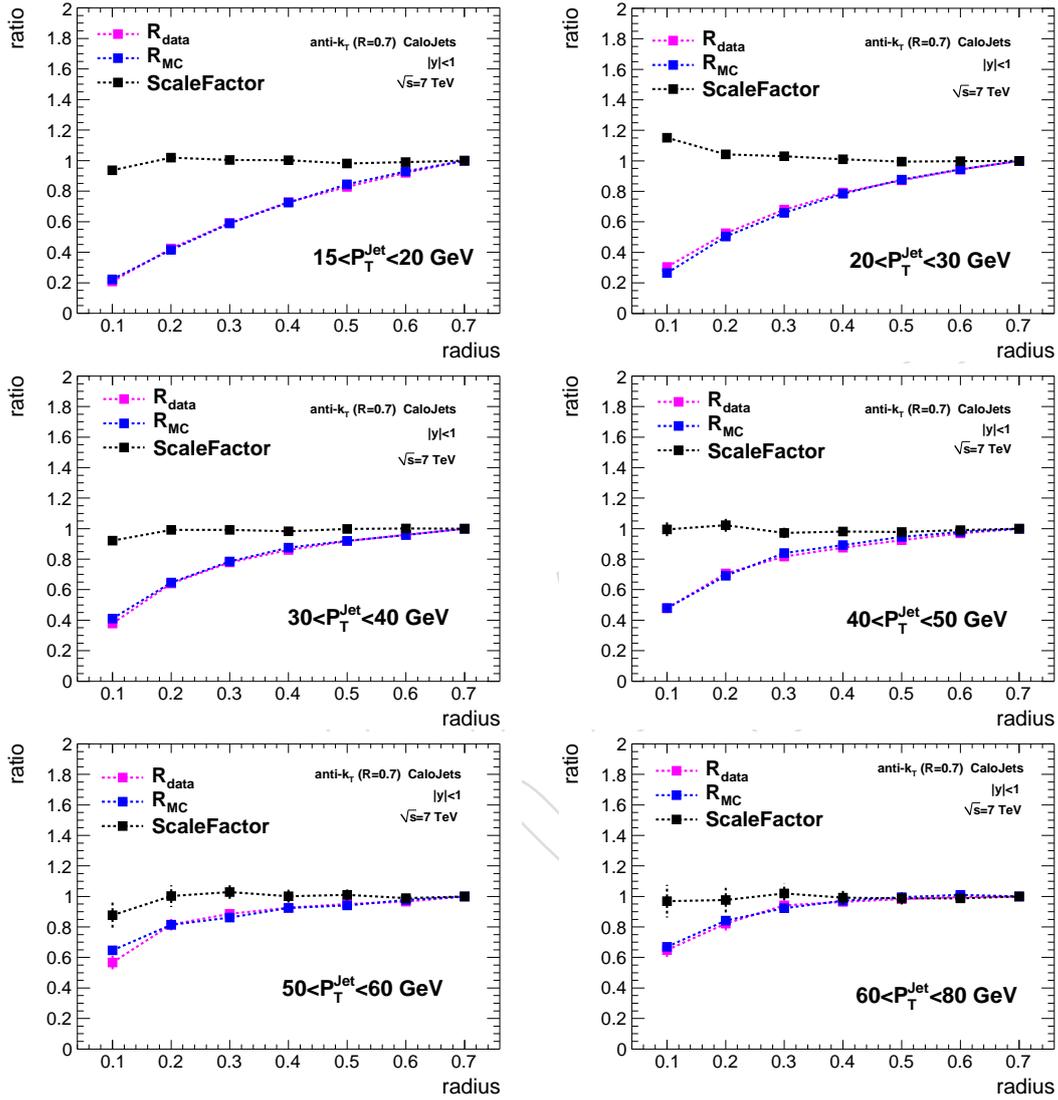


Figure 34: The fractional change in the differential jetshapes due to uncertainty in the jet energy scale determined by changing the jet energy scale by  $\pm 10\%$  independent of jet  $p_T$  and  $y$ .

275 scale, jet fragmentation and calorimeter simulation effects. The total systematic uncertainty at  
276  $r=0.2$  is 12% at  $p_T = 60$  GeV, decreasing to 4% at jet  $p_T = 1$  TeV.

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GeV	$N^{jets}$	$N_p$	$\langle \psi(r = 0.2) \rangle$	$rms$	$\sigma = rms / \sqrt{N_p}$	$\sigma / \langle \psi(r = 0.2) \rangle$ (%)
15-20	5313					
20-30	4333					
30-40	1147					
40-50	403					
50-60	210					
60-80	101					
80-100	41					
100-	16					

Table 1: Number of jets before and after prescale, and mean and rms values of the  $p_T$  fraction histograms at  $r=0.2$  in  $10 \text{ pb}^{-1}$  for all  $p_T$  jet bins which were analyzed. Statistical errors are listed for the corresponding jet  $p_T$  using prescaled event numbers.

Table 2: Different sources of systematics for  $\psi(r = 0.2)$  listed as percentage contributions for all jet  $p_T$  bins for  $10 \text{ pb}^{-1}$  of integrated luminosity. Total systematics is a quadrature sum of fragmentation, jet energy scale, showering and  $E/p$  contributions.

$p_T$ (GeV)	Fragmentation(%)	JES(%)	Showering(%)	$E/p$ (%)	TotalSys.(%)
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Table 3: Absolute error on  $1 - \psi(r = 0.2)$  represents quadratic sum of systematic and statistical uncertainties for  $10 \text{ pb}^{-1}$  of integrated luminosity.  $I(r = 0.2)$  refers to the integrated correction factors at  $r=0.2$ .

$p_T$ GeV	Raw $\psi(r = 0.2)$	$I(r = 0.2)$	$1 - \psi(r = 0.2)$	AbsErr
15 - 20	0.66	0.90	0.41	0.072

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306 momentum  $P_T$  is defined as a projection of a particle momentum  $P$  on the  $xy$ -plane,  
307  $P_T = P \cdot \sin \theta$ . The rapidity is defined as  $y = \frac{1}{2} \log \frac{E+P_z}{E-P_z}$ , where  $E$  denotes the energy and  
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