

Dark Matter and Electroweak Baryogenesis

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based on works done in collaboration with:

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Outline

- **The Standard Model: its glory and shortcomings**
- **Evidence for Dark Matter and its possible origin**
- **The Puzzle of matter-antimatter asymmetry**

- **Baryogenesis at the Electroweak scale**
 - ➔ **in the SM: ruled out!**
 - ➔ **in the minimal SUSY extension of the SM:
constraints on the SUSY spectrum and extra CP violation**

- **SUSY Dark matter and electroweak baryogenesis**
 - ★ **regions of neutralino relic density compatible with WMAP**
 - ★ **experimental tests at colliders**
 - ★ **direct dark matter detection**

- **Conclusions**

The Standard Model: the pillar of particle physics

- describes physical processes up to energies of about 100 GeV
- explains data collected in the past several years
with very high precision (one part in a thousand)

Open questions in the Standard Model

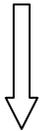
- Source of **Mass** of fundamental particles.
- Origin of the observed asymmetry between particles and antiparticles (**Baryon Asymmetry**).
- Nature of the **Dark Matter**, contributing to most of the matter energy of the Universe.
- **Quantum Gravity** and Unified Interactions.

Evidence for Dark Matter:

Visible stars do not account for enough mass to explain the rotation curves of galaxies

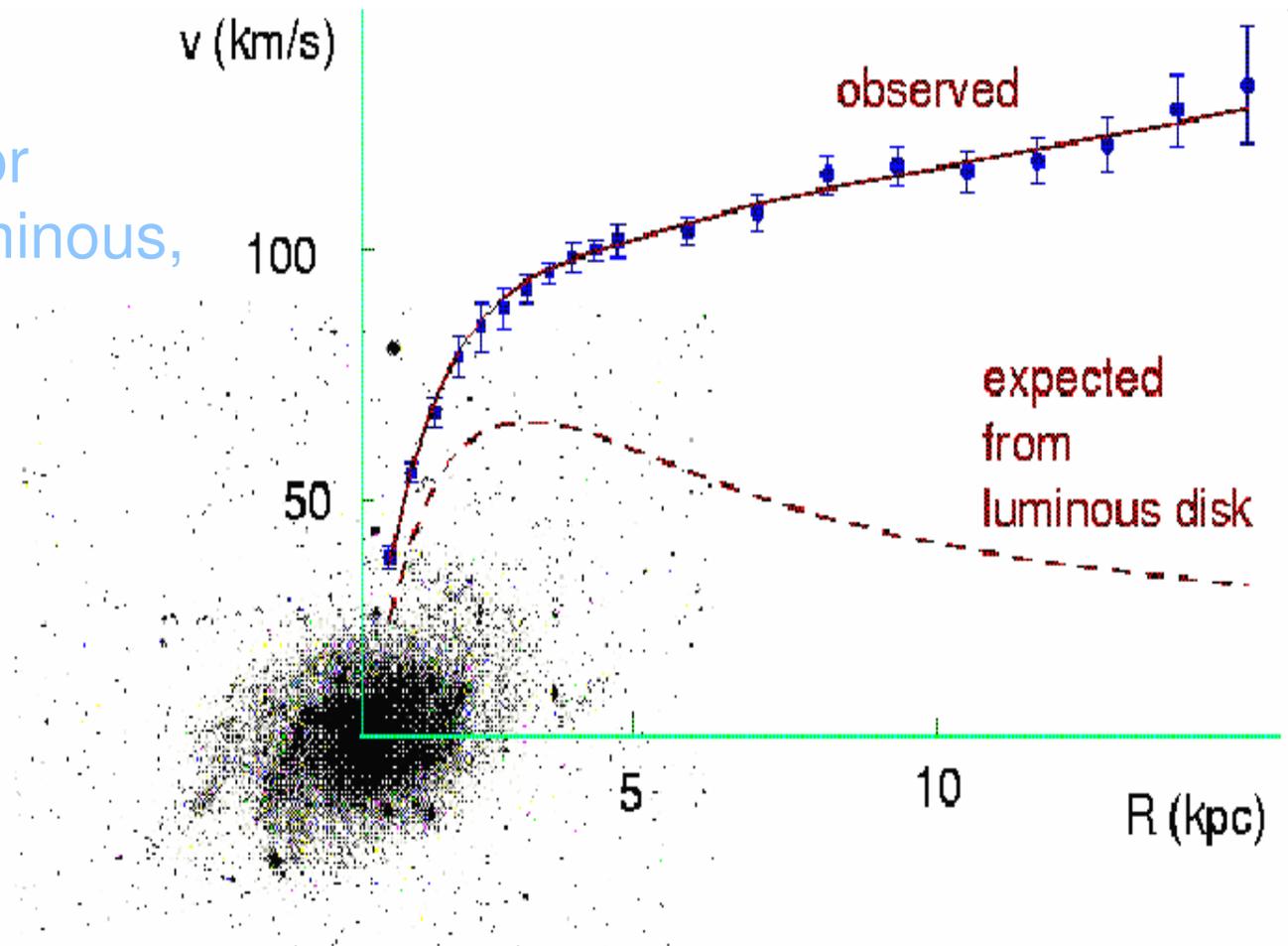
Gravity prediction:
$$\frac{v^2}{r} = G_N \frac{M(r)}{r^2} \Rightarrow v^2 \propto \frac{1}{r}$$

Strong evidence for additional, non-luminous, source of matter:



Dark Matter

Zwicky, 1930s



Cosmic Microwave Background

WMAP measures the **CMB** and determines

$$\Omega_M h^2 = 0.135 \pm 0.009 \quad \Omega_B h^2 = 0.0224 \pm 0.0009 \quad h = 0.71 \pm 0.04$$

difference gives CDM energy density: $\Omega_{\text{CDM}} h^2 = 0.1126 \pm_{0.0181}^{0.0161}$

What is Dark Matter? The SM has no suitable candidates

- leptons, hadrons: too little
- photons: $\Omega_{\text{rad.}} \approx 10^{-4}$
- neutrinos: too light
- W/Z bosons: too unstable
- **Dark matter must be *something* beyond the SM!**

Possible origin of Dark Matter

- Weakly interacting particles (WIMPS), with masses and interaction cross sections of order of the electroweak scale
→ most compelling alternative

Relic Density

- To estimate WIMPs relic density, assume it was in thermal equilibrium in the early universe:

$$n_{eq} = g \left(\frac{mT}{2\pi} \right)^{3/2} \text{Exp} \left[-m/T \right]$$

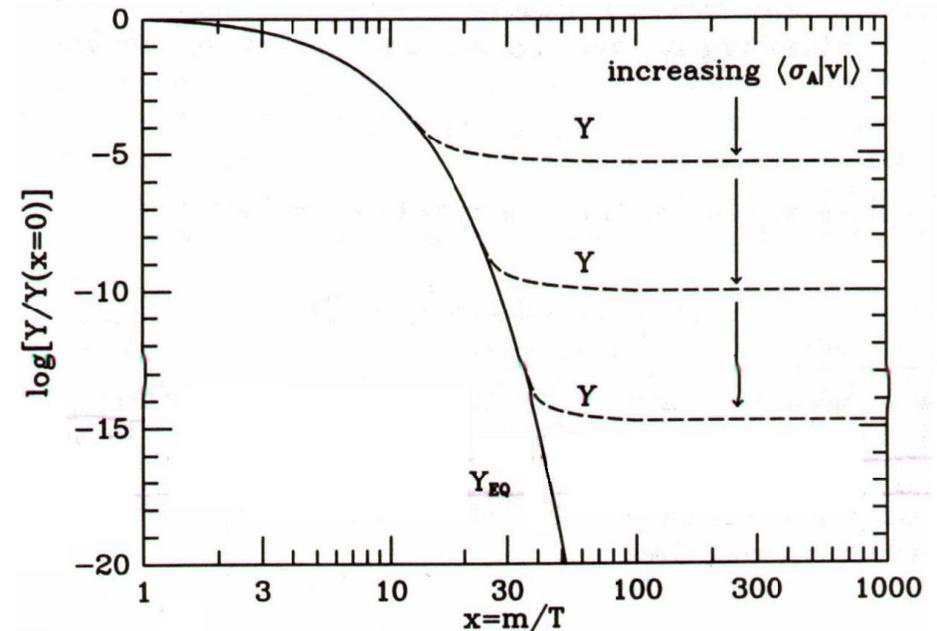
- Interactions with the relativistic plasma are efficient, but the WIMPs follow a Maxwell-Boltzmann distribution. **However, the universe is expanding, and once the density is small enough, they can no longer interact with one another, and fall out of equilibrium.**

Below the freeze-out temperature, the WIMPs density per co-moving volume is fixed

$$\frac{dY}{dx} = - \frac{\langle \sigma v \rangle}{H x} s (Y^2 - Y_{eq}^2)$$

with $Y = n/s$ and $x = m/T$

The key ingredient is the thermally annihilation cross section:
density is inversely proportional to it.



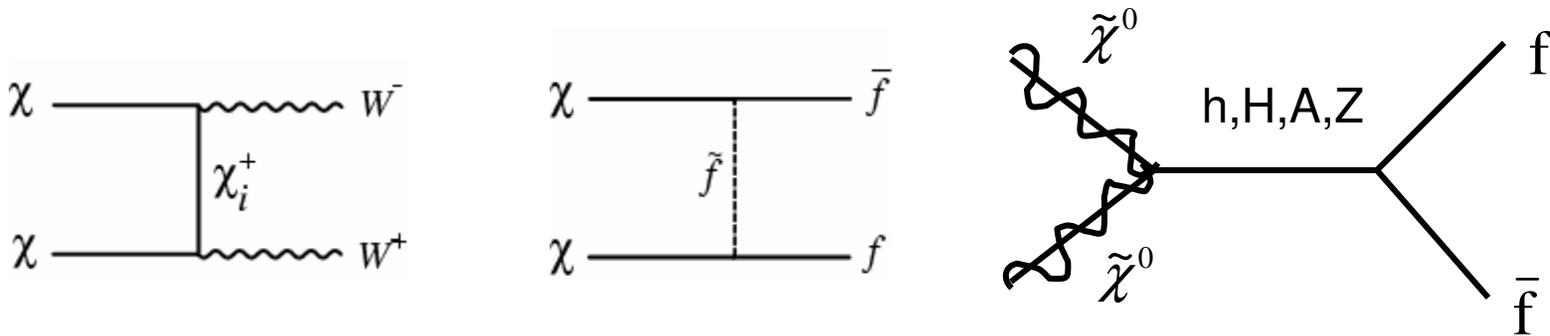
Kolb and Turner

Supersymmetry:

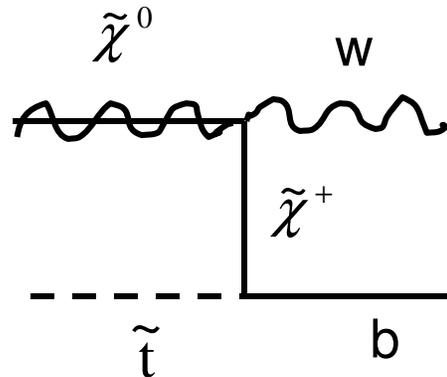
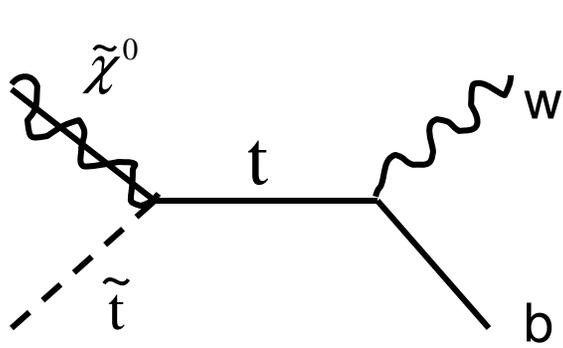
with R parity discrete symmetry conserved $P = (-1)^{3B+L+S}$

naturally provides a stable, neutral, dark matter candidate: the lightest neutralino $\tilde{\chi}^0$

Many processes contribute to the neutralino annihilation cross section



If any other SUSY particle has mass close to the neutralino LSP, it may substantially affect the relic density via co-annihilation



if stops NLSP
neutralino-stop
co-annihilation

The Puzzle of the Matter-Antimatter asymmetry

- Anti-matter is governed by the same interactions as matter.
- Observable Universe is mostly made of matter: $N_B \gg N_{\bar{B}}$
- Anti-matter only seen in cosmic rays and particle physics accelerators
The rate observed in cosmic rays consistent with secondary emission of antiprotons $N_{\bar{p}} \approx 10^{-4} N_p$

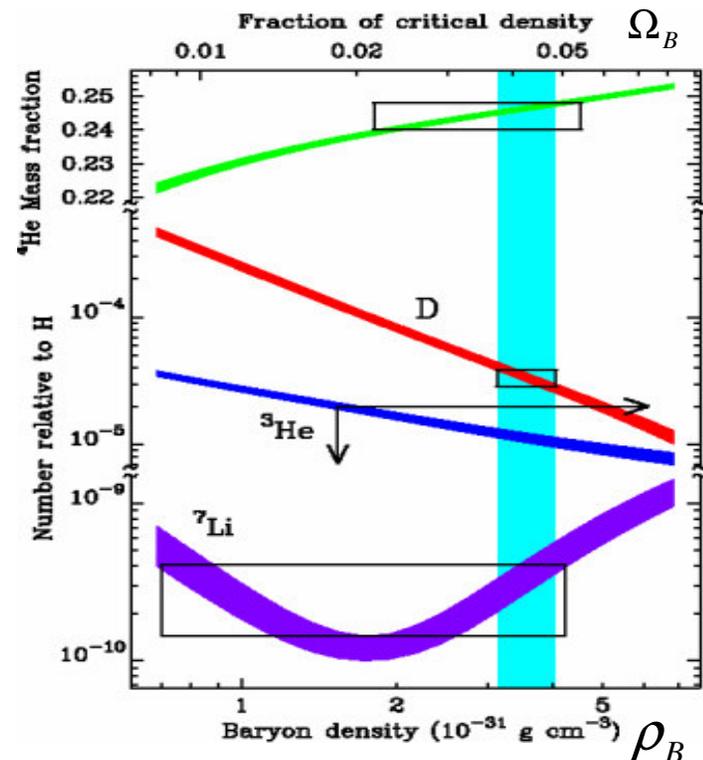
Information on the baryon abundance:

- Abundance of primordial elements combined with predictions from Big Bang Nucleosynthesis:

$$\eta = \frac{n_B}{n_\gamma}, \quad n_\gamma = \frac{421}{\text{cm}^3}$$

- CMBR:

$$\frac{\rho_B}{\rho_c} \equiv \Omega_B, \quad \rho_c \approx 10^{-5} h^2 \frac{\text{GeV}}{\text{cm}^3}$$



Baryon-Antibaryon asymmetry

- Baryon Number abundance is only a tiny fraction of other relativistic species

$$\eta = \frac{n_B}{n_\gamma} = 2.68 \cdot 10^{-8} \Omega_B h^2 \approx 6 \cdot 10^{-10}$$

- In early universe B, \bar{B} and γ 's were equally abundant. B, \bar{B} annihilated very efficiently. No net baryon number if B would be conserved at all times. What generated the small observed baryon antibaryon asymmetry ?

Sakharov's Requirements:

- ✦ Baryon Number Violation (any B conserving process: $N_B = N_{\bar{B}}$)
- ✦ C and CP Violation: $(N_B)_{L,R} \neq (N_{\bar{B}})_{L,R}$
- ✦ Departure from thermal equilibrium

All three requirements fulfilled in the SM

In the SM Baryon Number conserved at classical level but violated at quantum level : $\Delta B = \Delta L$

*Anomalous processes violate both B and L number, but preserve B-L.
(Important for leptogenesis idea)*

- *At $T = 0$, Baryon number violating processes exponentially suppressed*

$$\Gamma_{\Delta B \neq 0} \cong \exp(-2\pi / \alpha_w)$$

- *At very high temperatures they are highly unsuppressed,*

$$\Gamma_{\Delta B \neq 0} \propto T$$

- *At Finite Temperature, instead, only Boltzman suppressed*

$$\Gamma_{\Delta B \neq 0} \cong \beta_0 T \exp(-E_{\text{sph}}(T) / T)$$

with $E_{\text{sph}} \cong 8 \pi v(T) / g$ and $v(T)$ the Higgs v.e.v.

Origin of Baryon asymmetry \longrightarrow essentially two possibilities

- **Baryon asymmetry generated at high energies**

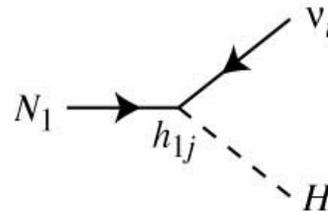
\longrightarrow through the decay of heavy particles, out of equilibrium, with

CP violation: to generate more B than anti B

$B-L \neq 0$: to avoid washout of generated B asymmetry via sphaleron processes

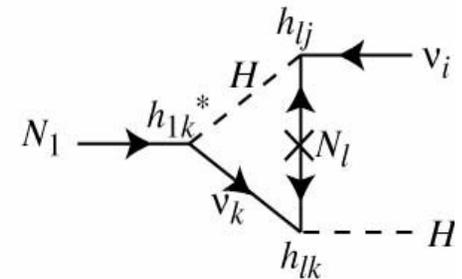
Leptogenesis: B number generated from L number plus anomaly interactions which convert L into B (Fukugita, Yanagida)

- Heavy, right-handed neutrinos decay out-of-equilibrium



- CP violating phases appear in the interference between the tree-level and one-loop amplitudes.

- Detailed calculation shows that lightest right handed neutrino mass should be $M_N \geq 10^{10} \text{ GeV}$ to obtain proper baryon asymmetry.



Needs heavy Majorana neutrinos, which are used in the standard explanation for neutrino masses: Seesaw Mechanism: small mass eigenvalue demands very large M_N

• Baryogenesis at the Electroweak Phase transition

- Start with $B=L=0$ at $T > T_c$
- CP violating phases create chiral baryon-antibaryon asymmetry in the symmetric phase. Sphaleron processes create net baryon asymmetry.
- Net Baryon Number diffuse in the broken phase

if $n_B = 0$ at $T > T_c$, independently of the source of baryon asymmetry

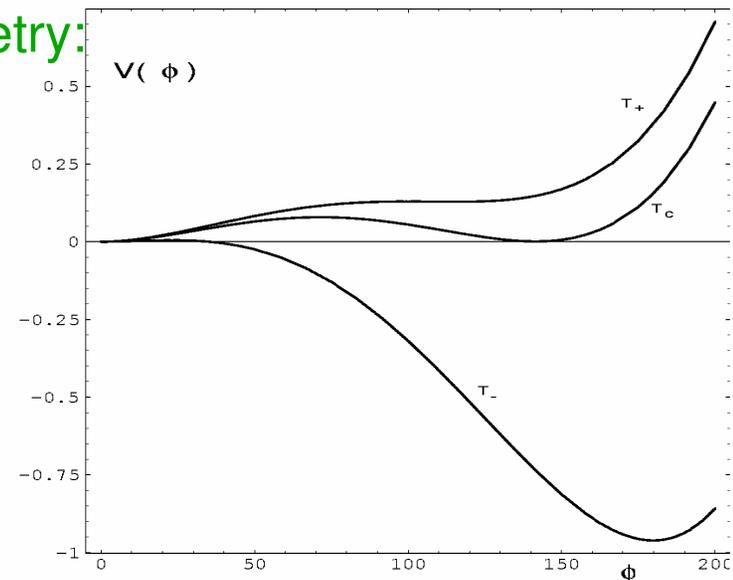
$$\frac{n_B}{s} = \frac{n_B(T_c)}{s} \exp\left(-\frac{10^{16}}{T_c(\text{GeV})} \exp\left(-\frac{E_{\text{sph}}(T_c)}{T_c}\right)\right)$$

To preserve the generated baryon asymmetry:

strong first order phase transition:

$$v(T_c) / T_c > 1$$

Baryon number violating processes out of equilibrium in the broken phase



SM Electroweak Baryogenesis fulfills the Sakharov conditions

- **Baryon number violation: Anomalous Processes**
- **CP violation: Quark CKM mixing**
- **Non-equilibrium: Possible at the electroweak phase transition.**

Finite Temperature Higgs Potential

$$V_{\text{eff}}^{\text{SM}} = -m^2(T) H^2 + E_{\text{SM}} T H^3 + \lambda(T) H^4$$

a cubic term is induced, proportional to the sum of the cube of all light boson particle masses

$$- \sum_b \frac{m_b^3(H)}{12\pi} T \quad \text{with} \quad m_b^2(H) \approx g_{bH}^2 H^2$$

In general: $m_b^2(H, T) = m_b^2 + g_{bH}^2 H^2 + \Pi(T)$ which can spoil the behaviour of the cubic term therefore jeopardizing first order first transition

In the SM the only contribution comes from the longitudinal components of the gauge bosons

$$E_{\text{SM}} \approx \frac{2}{3} \left(\frac{2M_W^3 + M_Z^3}{\sqrt{2}\pi v^3} \right)$$

→ hence a first order first transition occurs

$$\frac{v(T_c)}{T_c} \approx \frac{E}{\lambda}, \quad \text{with} \quad \lambda \propto \frac{m_H^2}{v^2}$$

the quartic coupling is proportional to the square of the Higgs mass

$$\frac{v(T_c)}{T_c} > 1 \quad \text{implies} \quad m_H < 40 \text{ GeV} \Rightarrow \text{ruled out!}$$

- **Independent Problem: not enough CP violation**

Electroweak Baryogenesis in the SM is ruled out

EW baryogenesis needs new light bosonic degrees of freedom with relevant couplings of the Higgs. The Higgs boson should remain light

Supersymmetry provides a natural framework:

each SM chiral fermion has a complex scalar with identical quantum numbers (besides the spin)

relevant light bosons: SUSY partners of the top quark = stops

In the **Minimal Supersymmetric extension of the Standard Model**:

- two Higgs doublets H_1 and H_2 necessary $\Rightarrow \tan \beta = v_2 / v_1$
- Its neutral scalar components acquire v.e.v.'s: v_1, v_2
with $v^2 = v_1^2 + v_2^2 = 246 \text{ GeV}$ determined by gauge boson masses:

5 physical states remain: 2 CP-even **h, H** with mixing angle α
1 CP-odd **A** and a charged pair **H^\pm**

If $m_A \gg m_Z$



decoupling limit

- lightest Higgs has SM-like couplings and mass below 135 GeV
- other Higgs bosons heavy and roughly degenerate

Light Stop Effects on Electroweak Baryogenesis

The left- and right-handed stops mix:

$$M_{\tilde{t}}^2 = \begin{bmatrix} m_Q^2 + m_t^2 + D_L & m_t X_t \\ m_t X_t & m_U^2 + m_t^2 + D_R \end{bmatrix}$$

$$\text{with } X_t = A_t - \frac{\mu^*}{\tan\beta}$$

$$\text{and } m_t = h_t H_2 = h_t \sin\beta \phi$$

Hierarchy in soft SUSY breaking param:

$$m_Q^2 \gg m_U^2 \implies \text{best fit to precision electroweak data}$$

$$\text{The lightest stop} \implies m_{\tilde{t}}^2(T=0) \approx m_U^2 + D_R + m_t^2 \left(1 - \frac{X_t^2}{m_Q^2} \right)$$

has six degrees of freedom and a coupling of order one to the Higgs

$$V_{eff}^{MSSM} = -m^2(T) \phi^2 - T \left[E_{SM} \phi^3 + 2N_c \frac{(m_{\tilde{t}}^2 + \Pi_R(T))^{3/2}}{12\pi} \right] + \frac{\lambda(T)}{2} \phi^4$$

No stop contrib. to cubic term unless $m_U^2 + \Pi_R(T) \approx 0$, very light right-h. stop!

In the MSSM:
$$E_{\text{MSSM}} \approx E_{\text{SM}} + \frac{h_t^3 \sin^3 \beta}{2\pi} \left(1 - \frac{X_t^2}{m_Q^2} \right)^{3/2}$$

one stop should be quite light and the stop mixing moderate to enhance E_{MSSM}

- For small stop mixing: $E_{\text{MSSM}} \approx 9 E_{\text{SM}}$ hence $m_{h_{\text{MSSM}}}^{\text{max.}} \approx 3 m_{H_{\text{SM}}}^{\text{max.}} \approx 120 \text{ GeV}$
it can work!!

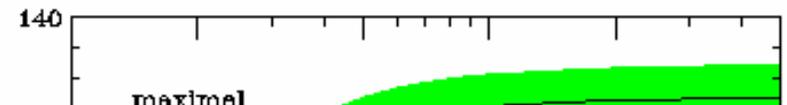
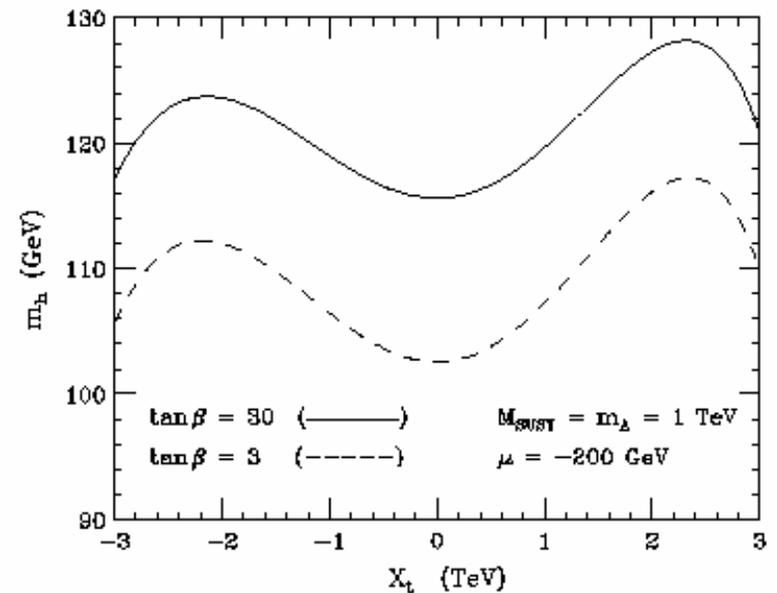
Present LEP bounds on the SM-like Higgs mass imply extra demands!

$$m_{H_{\text{SM-like}}} > 114.6 \text{ GeV}$$

- MSSM lightest Higgs mass depends crucially on m_t^4 , on the stop mixing X_t and logarithmically on the stop masses

$$m_h^2 \approx M_Z^2 \cos^2 2\beta + \frac{3m_t^4}{8\pi^2 v^2} \left[\log \left(\frac{m_{\tilde{t}_L}^2 m_{\tilde{t}_R}^2}{m_t^4} \right) + 2 \frac{|X_t|^2}{m_Q^2} \log \left(\frac{m_{\tilde{t}_H}^2}{m_{\tilde{t}_L}^2} \right) + \mathcal{O} \left(\frac{|X_t|^4}{m_Q^4} \right) \right]$$

hence $m_Q \geq 1 \text{ TeV}$ and $X_t \geq 0.3 m_Q$ needed



Higgs and Stop mass constraints for Electroweak Baryogenesis

- **Higgs masses up to 120 GeV**
- **The lightest stop must have a mass below the top quark mass.**

A same point in this plane corresponds to different values of the Higgs and stop param.: $\tan \beta$, X_t , m_U and m_Q

$$\tan \beta \geq 5, \quad m_Q \geq 1 \text{ TeV}, \quad X_t \geq 0.3 m_Q$$

➡ lower values lead to too small Higgs mass

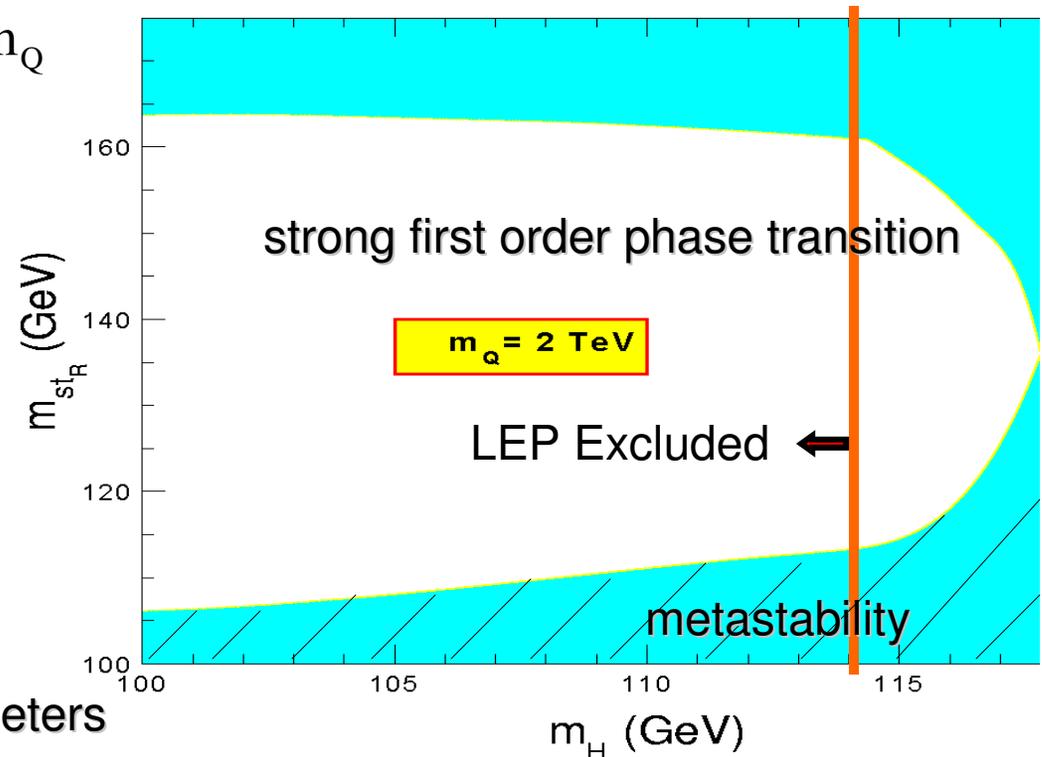
$$m_U \approx 0, \quad X_t \leq 0.5 m_Q$$

➡ to have a sufficiently strong first order first transition

conditions on the stop sector parameters

secure vacuum stability ↻

No color breaking minima



M.C, Quiros, Wagner

Computation of the baryon asymmetry

New CP violating phases in the stop and chargino sector are crucial
[for large values of $m_{\tilde{Q}}$, only the chargino –neutralino currents are relevant]

- Interaction with varying Higgs background in the bubble wall creates a net neutral and charged Higgsino current through CP-violating interactions
- Higgsino interactions with plasma creates an excess of left-handed anti-baryons (right-handed baryons)
- Left-handed baryon asymmetry is partially converted to lepton asymmetry via anomalous processes (weak sphalerons: net B violation)
- Baryon asymmetry diffuses into broken phase and gets frozen there since $v(T) / T > 1$

Assuming time relaxation of charge is large (no particle decays)

1. compute CP-violating currents
2. solve diffusion equations describing the above processes

Dependence of the Baryon asymmetry on SUSY parameters

Higgs sector : $\tan \beta$, m_A

Chargino sector : mass param. μ , M_2 with physical phase $\arg(\mu^* M_2)$

currents proportional to $\sin(\arg(\mu^* M_2))$, with resonant behavior for $M_2 \approx |\mu|$

Total Baryon asymmetry depends on two contributions proportional to:

$$\star \quad \varepsilon_{ij} H_i \partial_\mu H_j = v^2 (T) \partial_\mu \beta$$

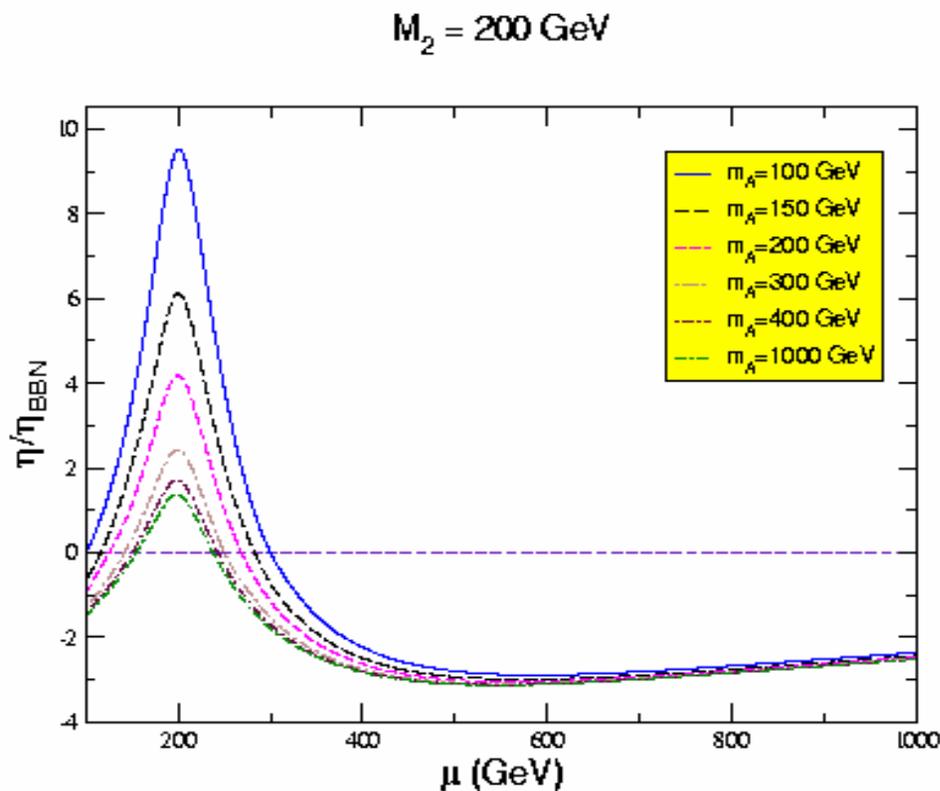
suppressed for large m_A and $\tan \beta$ due to $\Delta \beta$ dependence

$$\star \quad H_1 \partial_\mu H_2 + H_2 \partial_\mu H_1 = v^2 \cos(2\beta) \partial_\mu \beta + v \partial_\mu v \sin(2\beta)$$

unsuppressed for large CP-odd masses

Baryon Asymmetry Dependence on the Chargino Mass Parameters

M. Carena, M. Quiros,
M. Seco and C.W. '02



**Gaugino and Higgsino masses
of the order of the weak scale
highly preferred**

***Results for maximal
CP violation***

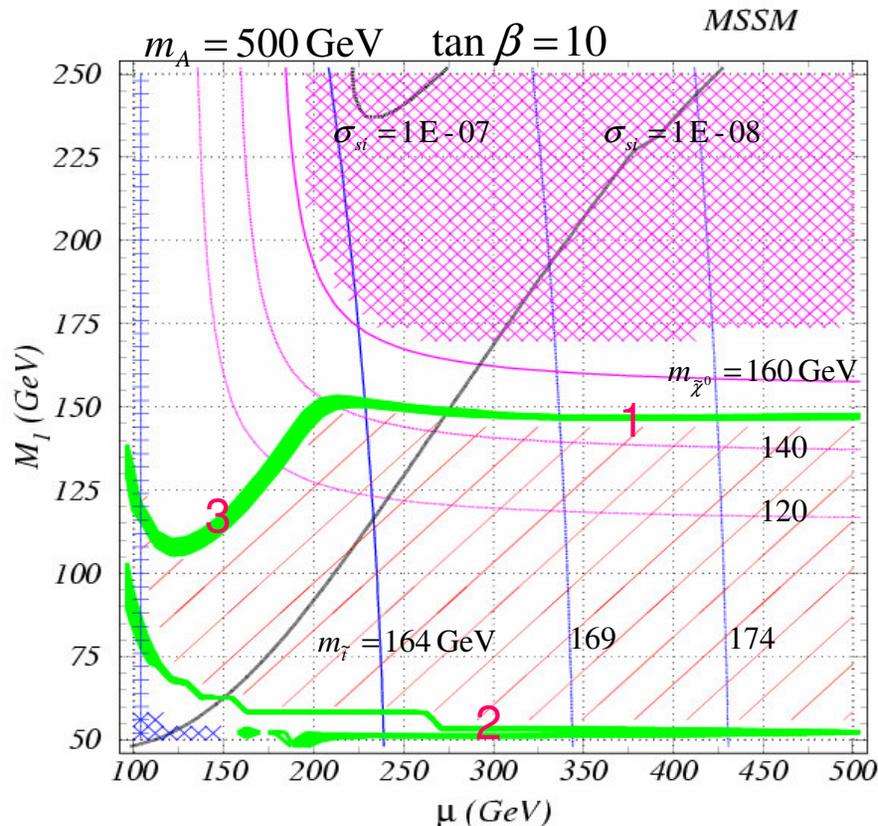
$$\sin(\arg(\mu^* M_2)) = 1$$

Baryon Asymmetry Enhanced for ; $M_2 = |\mu|$ and smaller values of m_A

**Even for large values of the CP-odd Higgs mass, acceptable values
obtained for phases of order one.**

Dark Matter and Electroweak Baryogenesis

- light right handed stop: $m_{\tilde{U}_3} \approx 0$ • heavy left handed stop: $m_{\tilde{Q}_3} \geq 1 \text{ TeV}$
- values of stop mixing compatible with Higgs mass constraints and with a strong first order phase transition: $X_t = \mu / \tan \beta - A_t = 0.3 - 0.5 m_{\tilde{Q}_3}$
- the rest of the squarks, sleptons and gluinos order TeV and $M_2 \cong 2M_1$



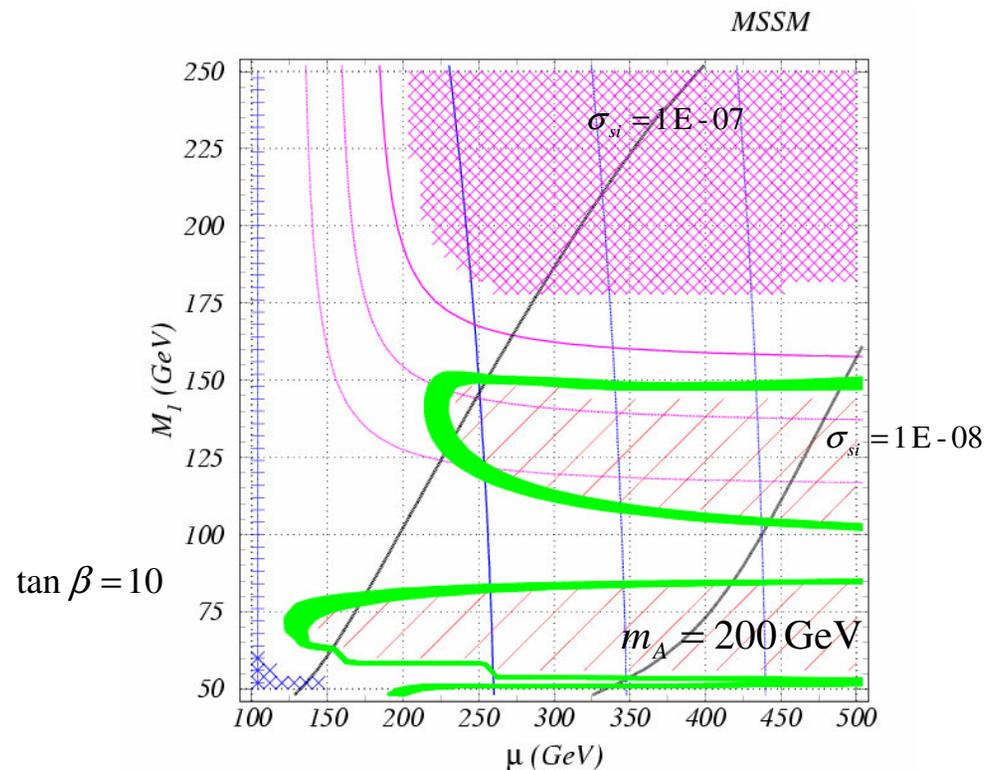
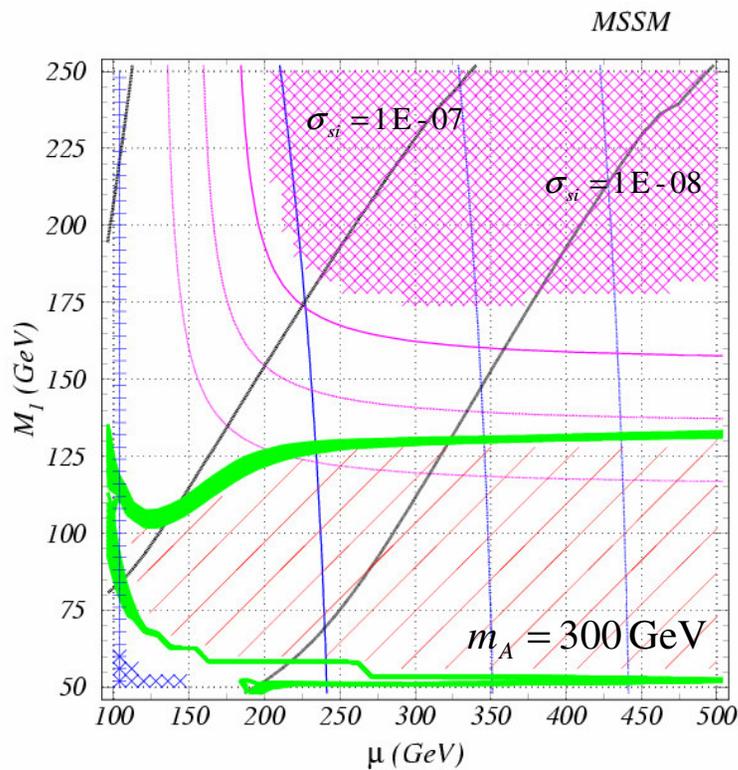
three interesting regions with neutralino relic density compatible with WMAP obs.
 $0.095 < \Omega_{\text{CDM}} h^2 < 0.129$ (green areas)

1. neutralino-stop co-annihilation: mass difference about 20-30 GeV
2. s-channel neutralino annihilation via lightest CP-even Higgs
3. annihilation via Z boson exchange
small μ and M_1

Heavy Higgs mass Effects

A,H contribute to annihilation cross section vis s-channel:

- $m_A = 300$ GeV main effect for values of neutralino mass close to stop mass, allowed region moves away from co-annihilation to lower neutralino masses
- $m_A = 200$ GeV new resonant region due to A,H s-channel (much wider band than for h due to $\tan \beta$ enhanced bb couplings). **Stop co-annihilation region reappears.**



- larger neutralino-proton scattering cross sections!

Balazs, MC, Wagner

Experimental Tests of Electroweak Baryogenesis and Dark Matter

- Higgs searches:

Higgs associated with electroweak symmetry breaking: SM-like.

Higgs mass below 120 GeV required

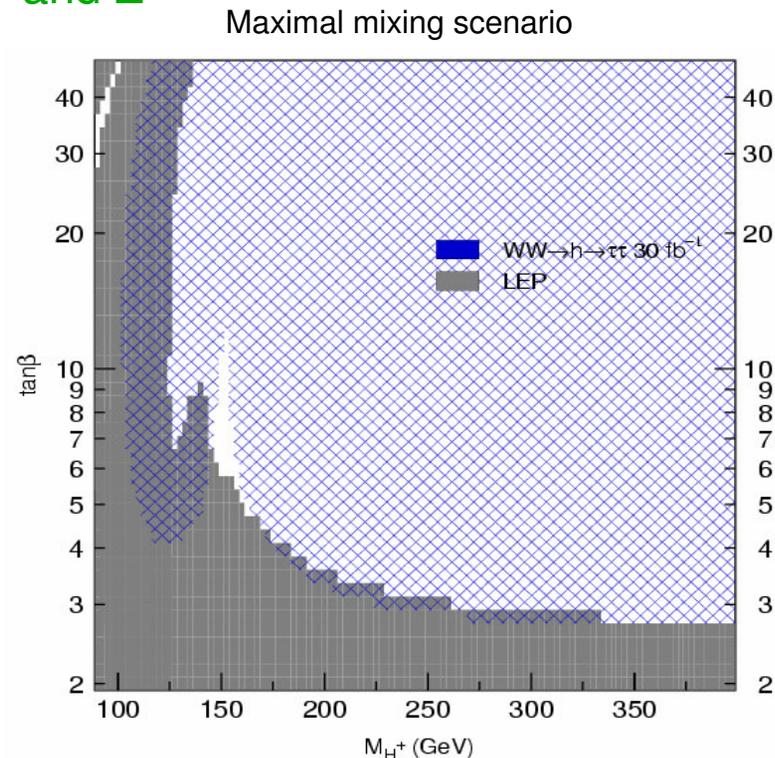
1. Tevatron collider may test this possibility: 3 sigma evidence with about 4 fb^{-1}

Discovery quite challenging, detecting a signal will mean that the Higgs has relevant strong (SM-like) couplings to W and Z

2. A definitive test of this scenario will come at the LHC with the first 30 fb^{-1} of data

$$qq \rightarrow qqV^*V^* \rightarrow qqh$$

$$\text{with } h \rightarrow \tau^+\tau^-$$



Searches for a light stop at the Tevatron

Light-stop models with neutralino LSP dark matter $\longrightarrow \cancel{E}_T$ signal

○ if $\tilde{t} \longrightarrow c\tilde{\chi}$ decay mode dominant and $\Delta_{m_{\tilde{t}\tilde{\chi}}} < 30$ GeV:
trigger on \cancel{E}_T crucial

$m_{\tilde{\chi}^0} < 100$ GeV and $m_{\tilde{t}} \leq 180$ GeV at reach if $\Delta_{m_{\tilde{t}\tilde{\chi}}} \geq 30$ GeV

$m_{\tilde{\chi}^0} \geq 120$ GeV then $m_{\tilde{t}}$ out of reach

- co-annihilation region not at Tevatron reach \rightarrow
- away from it strong dependence on the neutralino mass

○ if $m_{\tilde{t}} > m_{\tilde{\chi}} + m_W + m_b$ (3-body decay)

this always happens for

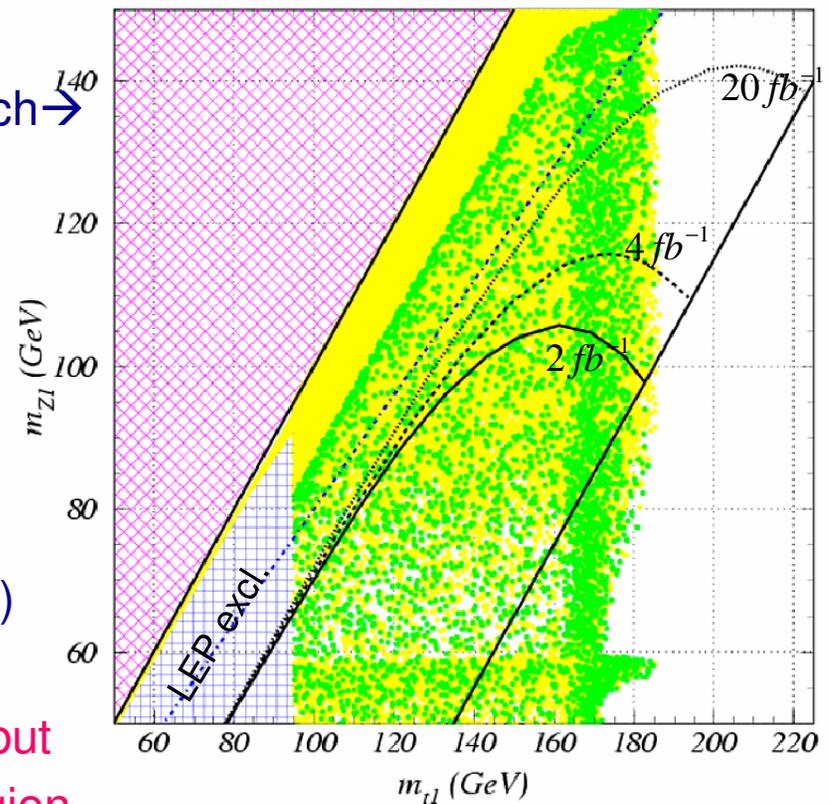
$$\text{(h-resonance)} \quad m_{\tilde{\chi}^0} \approx \frac{m_h}{2}$$

and $m_{\tilde{t}} \geq 140$ GeV no reach

(can search for charginos in trilepton channel)

LHC: good for chargino/neutralino searches but also difficulties for stops in co-annihilation region

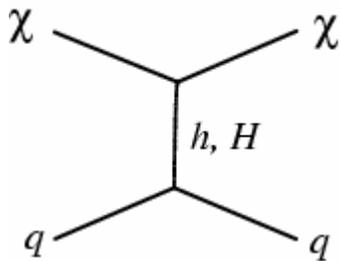
MSSM Balazs, MC, Wagner'04



Direct Dark Matter Detection

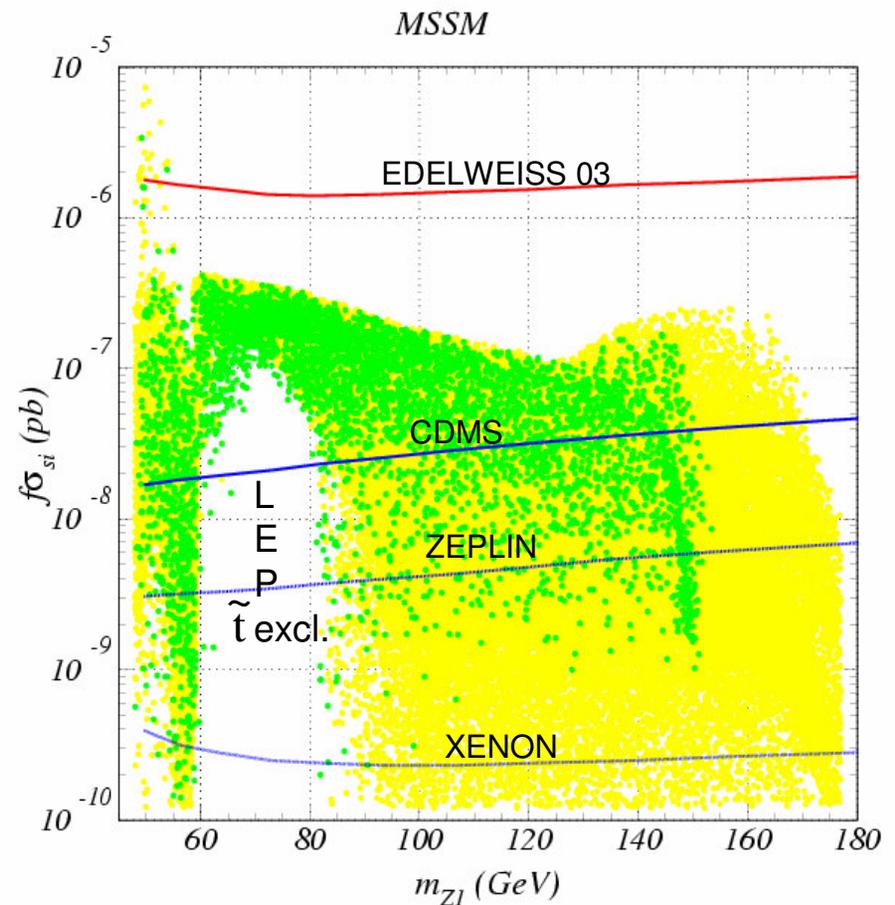
\cancel{E}_T at colliders \longrightarrow important evidence of DM candidate, but, stability of LSP on DM time scales cannot be checked at colliders

☀ Neutralino DM is searched for in neutralino-nucleon scattering exp. detecting elastic recoil off nuclei



\longrightarrow upper bounds on Spin independent cross sections

Next few years: $\sigma_{SI} \approx 10^{-8}$ pb
 Ultimate goal: $\sigma_{SI} \approx 10^{-10}$ pb (Fiorucci's talk)



small σ_{SI} for large μ : co-annihilation and h-resonant regions Balazs, MC, Wagner '04

Conclusions

- Supersymmetry with a light stop $m_{\text{stop}} < m_{\text{top}}$ and a SM-like Higgs with $m_h < 120$ GeV



opens the window for electroweak baryogenesis and allows for a new region of SUSY parameter space compatible with Dark Matter

also Gaugino and higgsino masses of order of the electroweak scale
and moderate CP-odd Higgs mass preferred
new CP violating phases: $\arg(\mu^* M_2) \geq 0.1$ necessary

*EWBG and DM in the MSSM → interesting experimental framework
stop-neutralino co-annihilation → challenging for hadron colliders*

Tevatron: good prospects in searching for a light stop

LHC: will add to these searches and explore the relevant $\tilde{\chi}^0 / \tilde{\chi}^\pm$ spectra

Stop co-annihilation region provides motivation to search in the small $\Delta_{m_{\tilde{\tau}\tilde{\chi}}}$ regime

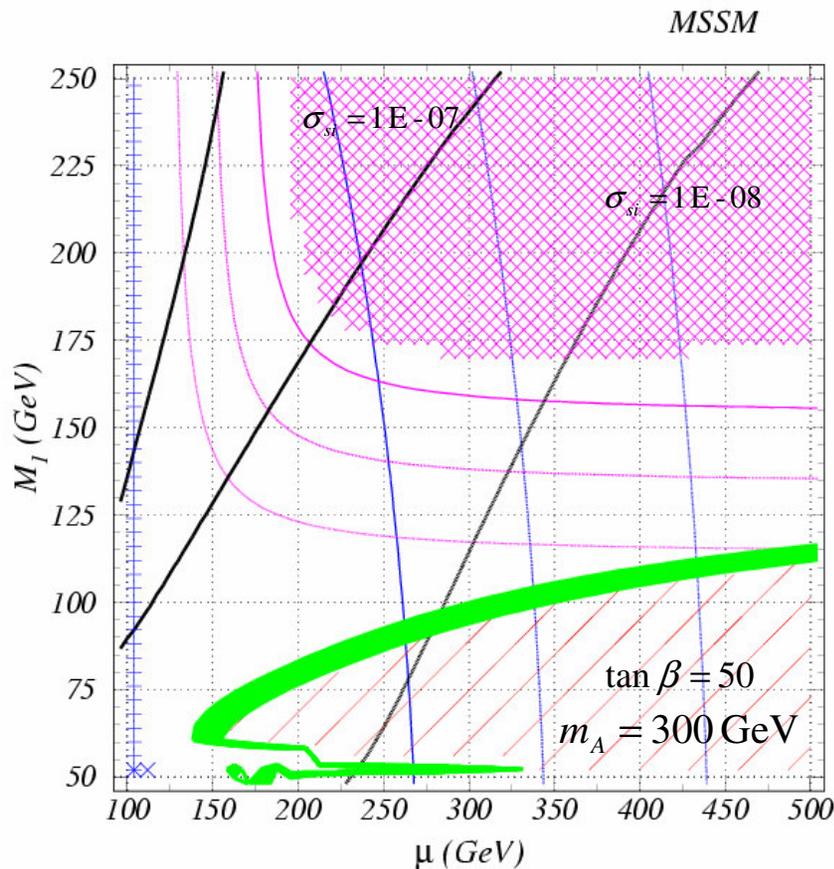
LC: important role in testing this scenario: small $\Delta_{m_{\tilde{\tau}\tilde{\chi}}}$ and nature and composition of light gauginos and stop

Direct Dark Matter detection: nicely complementary to collider searches

$\tan \beta$ Effects on the neutralino relic density

Main effect is via the coupling of the heavy Higgs A,H to bottom quarks

- annihilation cross section grows quadratically with $\tan \beta$



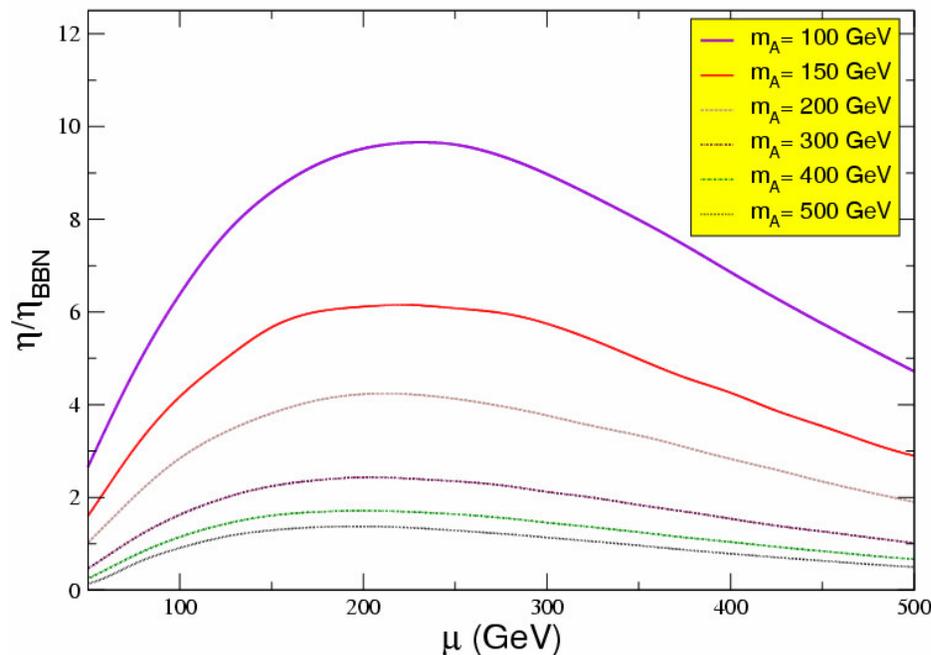
- For sufficiently small heavy Higgs masses and large tan beta:

$$m_A \approx 250 - 300 \text{ GeV} \quad \tan \beta \approx 50$$

can have dramatic consequences on the allowed region of parameter space

($m_A \approx 200 \text{ GeV}$ can make the relic density too small over most of the space)

- New sources of CP violation from the sfermion sector
- Generation of the baryon asymmetry: Charginos with masses μ and M_2 play most relevant role.
- CP-violating Sources depend on $\arg(\mu^* M_2)$
- Higgs profile depends on the mass of the heavy Higgs bosons $M_2 = \mu$



We plot for maximal mixing:
within uncertainties, values of
 $\sin \phi_\mu \geq 0.05$ preferred

Gaugino and Higgsino masses of the order of the weak scale highly preferred

Large CP-odd Higgs mass values are acceptable

Additional Topics

The Search for the Higgs Boson

If the Higgs Boson is created, it will decay rapidly into other particles

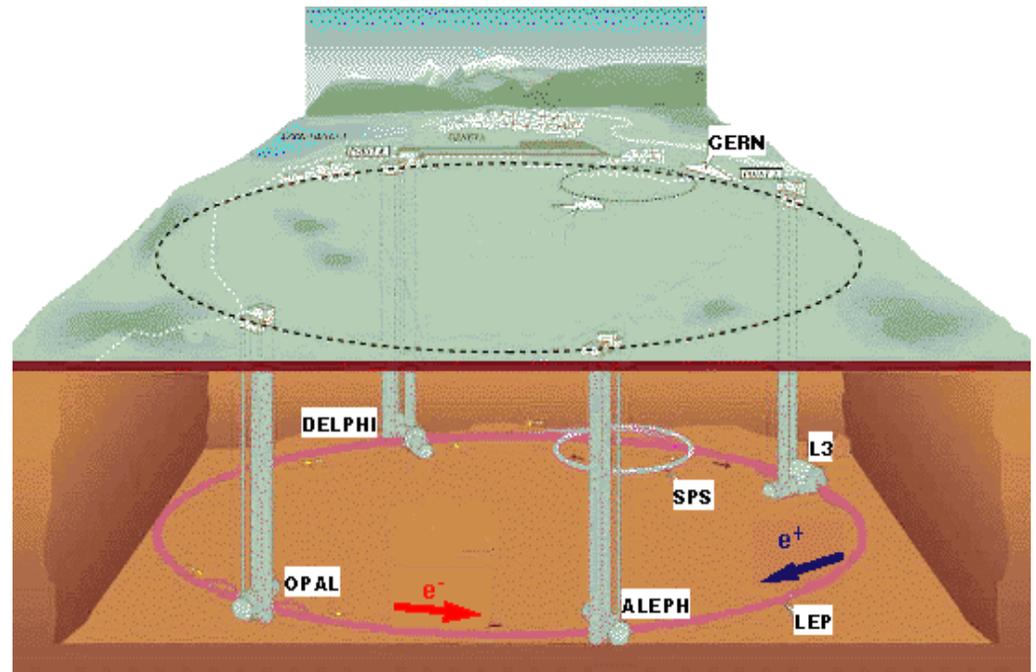
- The past: **The Large Electron Positron Collider - LEP**

$$e^+ e^- \xrightarrow{Z^*} H_{SM} Z$$

with $H_{SM} \rightarrow b\bar{b}, \tau^+ \tau^-$

and

$$Z \rightarrow q\bar{q}, l^+ l^-, \nu\bar{\nu}$$



In case of SUSY Higgs one can also search for

$$e^+ e^- \xrightarrow{Z^*} hZ, HZ, Ah, AH$$

Radiative corrections can have important impact on Higgs Branching ratios

Example: main decay mode $h \rightarrow b\bar{b}$ strongly suppressed in some MSSM regions

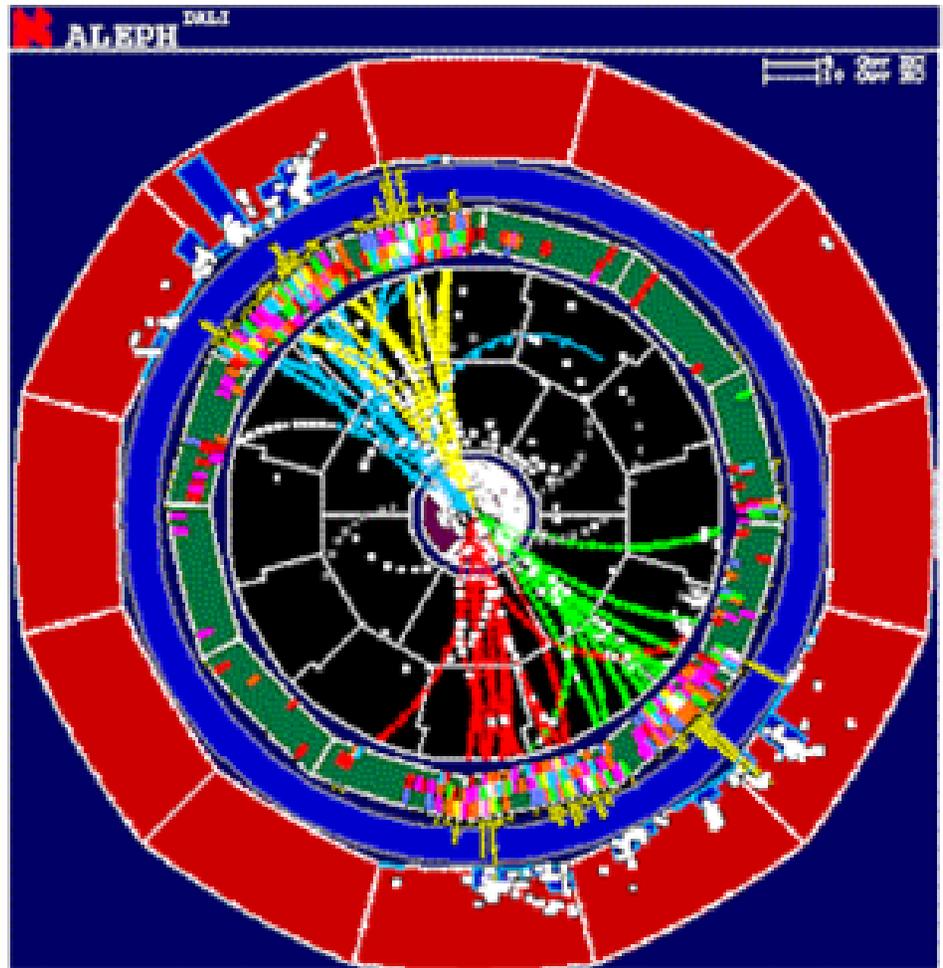
Higgs Particle Search at LEP (Aleph detector)

**Higgs candidate with
mass of about $114 \pm 3 \text{ GeV}$
and three identified b quarks**

SM Higgs Boson 95% C.L. limit

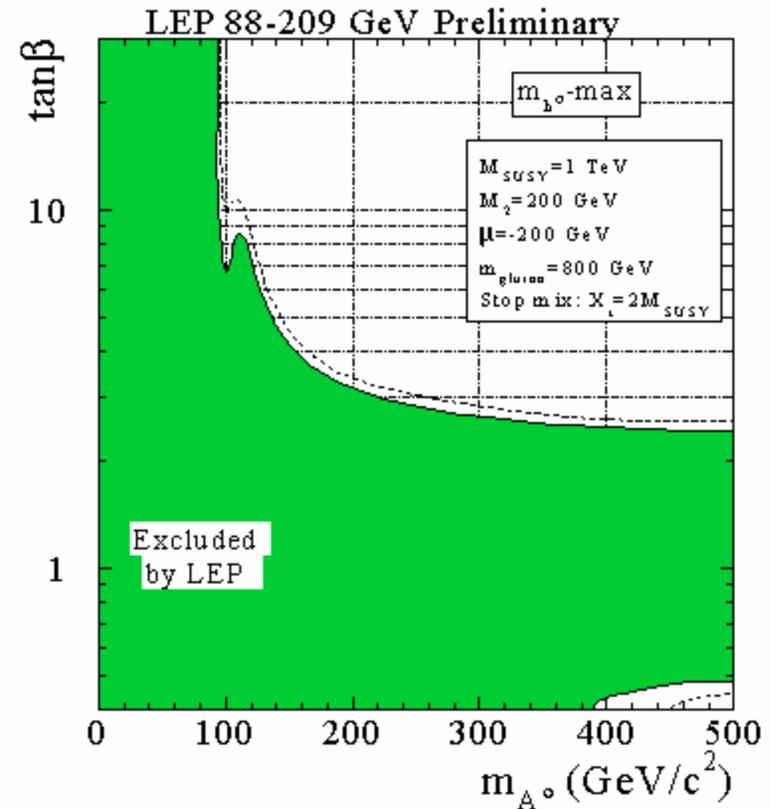
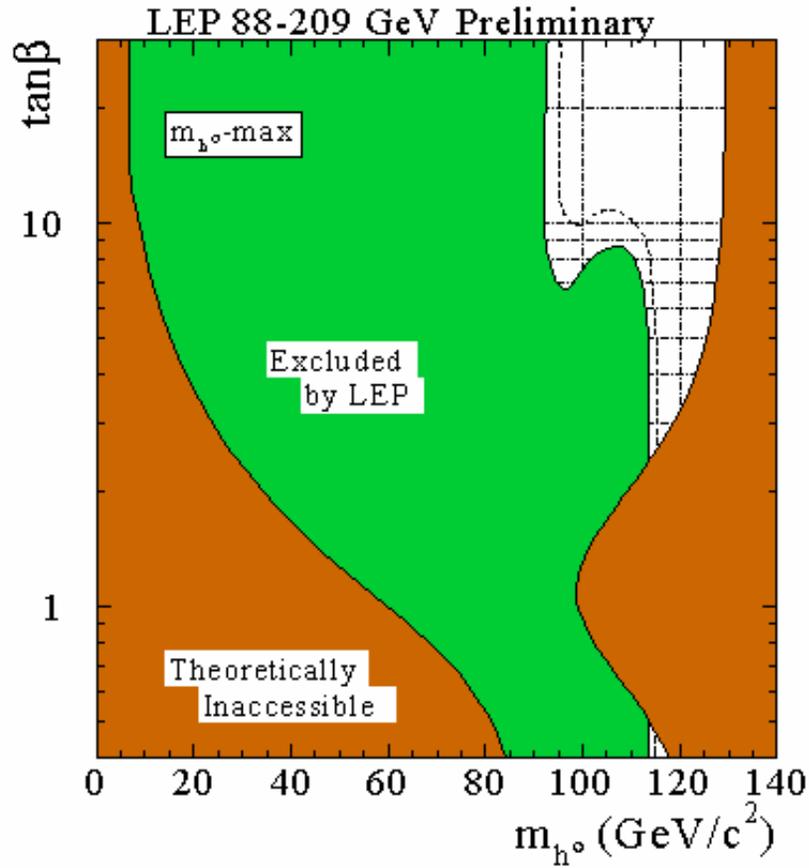
$$m_{H_{SM}} > 114.6 \text{ GeV}$$

**But, tantalizing hint of a Higgs
with mass about $115 - 116 \text{ GeV}$
(just at the edge of LEP reach)**



Present Status of MSSM Higgs searches

95%C.L. limits



MSSM Higgs $m_h > 91.0 \text{ GeV}; m_A > 91.9 \text{ GeV}$

Charged Higgs $m_{H^\pm} > 78.6 \text{ GeV}$ SM-like Higgs $m_h > 114.6 \text{ GeV}$

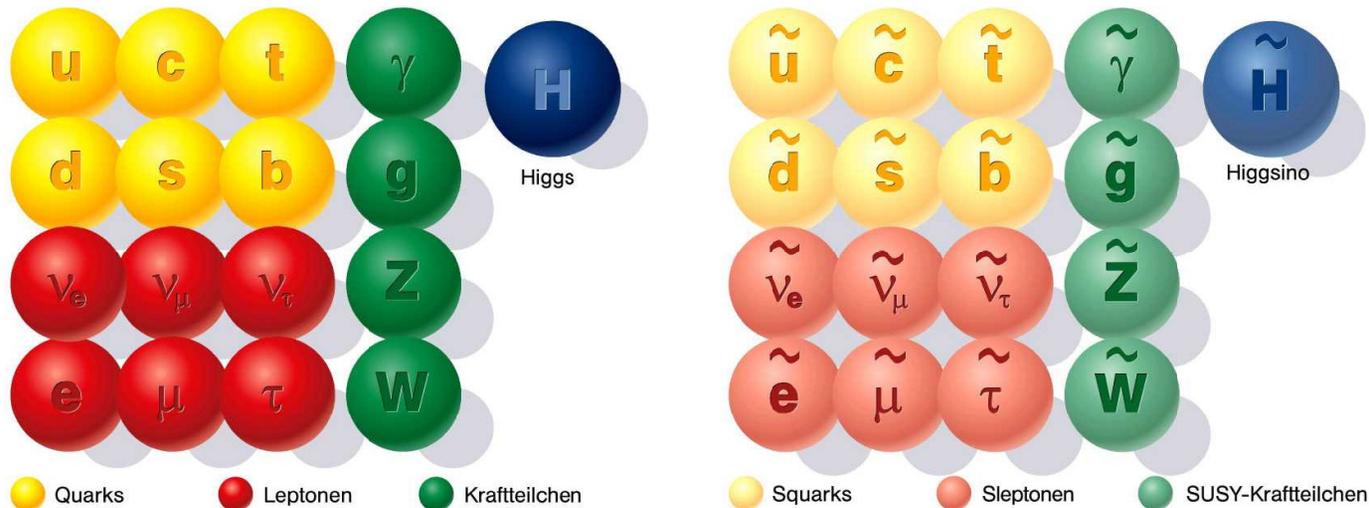
Low energy Supersymmetry

lesson from history: electron self energy \longrightarrow fluctuations of em fields generate a quadratic divergence but existence of electron antiparticle cancels it, otherwise QED will break down well below M_{Pl}

Will history repeat itself? Take SM and double particle spectrum

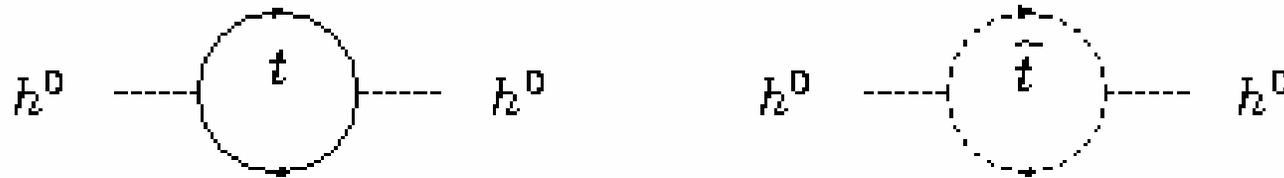
New Fermion-boson Symmetry: **SUPERSYMMETRY (SUSY)**

SM particles \longleftrightarrow **SUSY particles**



- Supersymmetric relations between couplings imply that $m_h \leq m_Z$

After quantum corrections, Higgs mass shifted due to incomplete cancellation of particles and superparticles in the loops



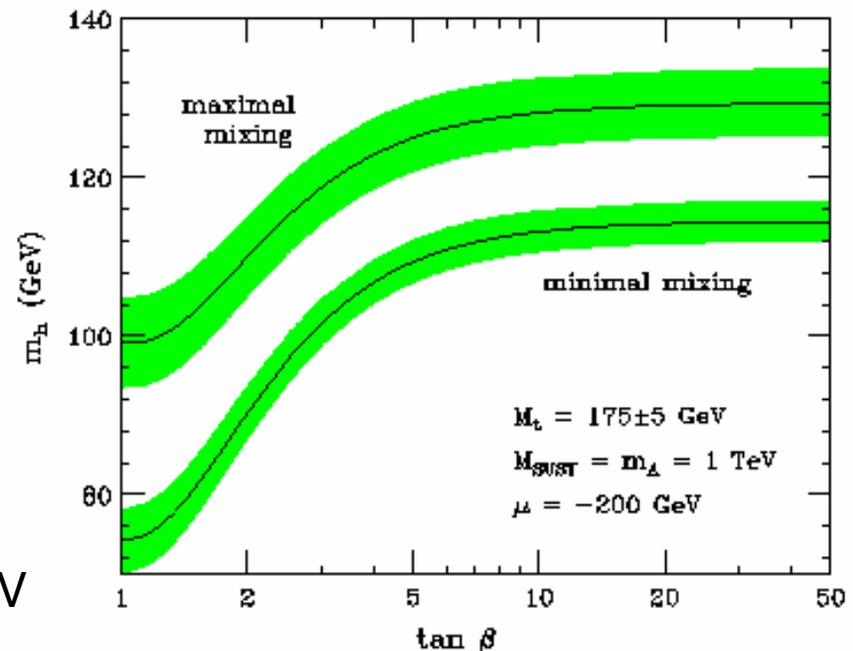
- Main Quantum effects:** m_t^4 enhancement ; dependence on the stop mixing X_t ; logarithmic sensitivity to the stop mass (averaged: M_S)

Upper bound :

$$m_h \leq 135 \text{ GeV}$$

stringent test of the MSSM

assuming M_S no heavier than 2 TeV



SM Electroweak Baryogenesis fulfills the Sakharov conditions

- **Baryon number violation: Anomalous Processes**
- **CP violation: Quark CKM mixing**
- **Non-equilibrium: Possible at the electroweak phase transition.**

Finite Temperature Higgs Potential

$$V = D(T^2 - T_0^2)H^2 + ET H^3 + \lambda H^4$$

E receives contributions proportional to the sum of the cube of all light boson particle couplings

$$\frac{v(T_c)}{T_c} \approx \frac{E}{\lambda}, \quad \text{with} \quad \lambda \propto \frac{m_H^2}{v^2}$$

Since in the SM the only bosons are the gauge bosons, and the quartic coupling is proportional to the square of the Higgs mass

$$\frac{v(T_c)}{T_c} > 1 \quad \text{implies} \quad m_H < 40 \text{ GeV} \Rightarrow \text{ruled out!}$$

- **Independent Problem: not enough CP violation**

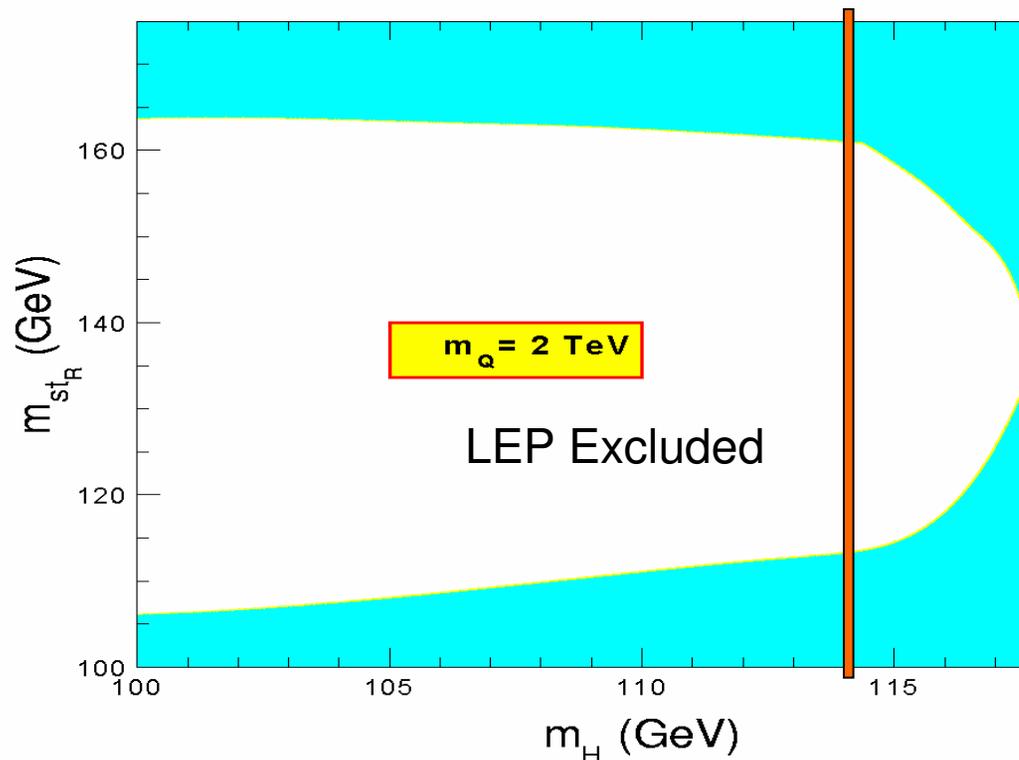
Electroweak Baryogenesis in the SM is ruled out

In the MSSM:

- New bosonic degrees of freedom: superpartners of the top quark, with strong couplings to the Higgs. $\Rightarrow E_{SUSY} \approx 8 E_{SM}$

Sufficiently strong first order phase transition to preserve generated baryon asymmetry:

- **Higgs masses up to 120 GeV**
- **The lightest stop must have a mass below the top quark mass.**



M.C, Quiros, Wagner

Cosmic Microwave Background

WMAP measures the CMB and determines

$$\Omega_M h^2 = 0.135 \pm 0.009 \quad \Omega_B h^2 = 0.0224 \pm 0.0009 \quad h = 0.71 \pm 0.04$$

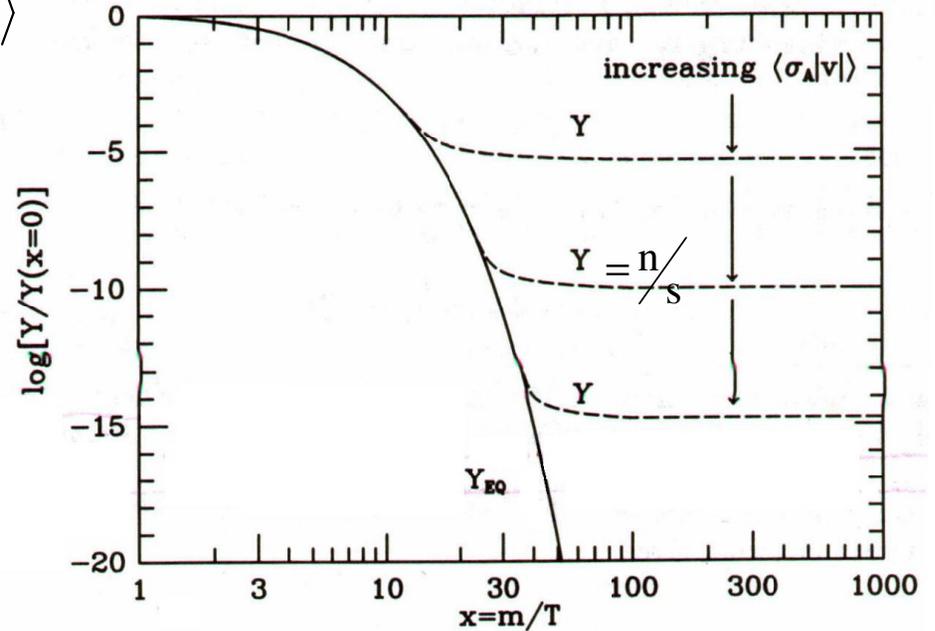
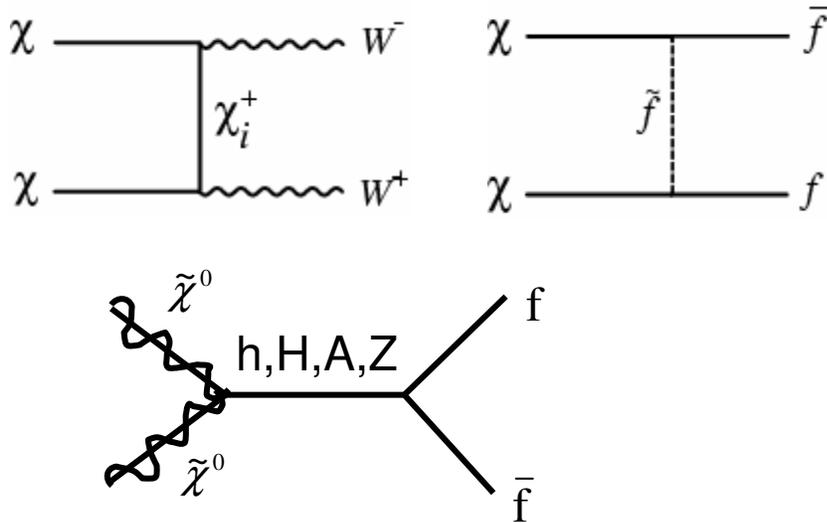
difference gives CDM energy density: $\Omega_{\text{CDM}} h^2 = 0.1126 \pm_{0.0181}^{0.0161}$

Possible origin of Dark Matter

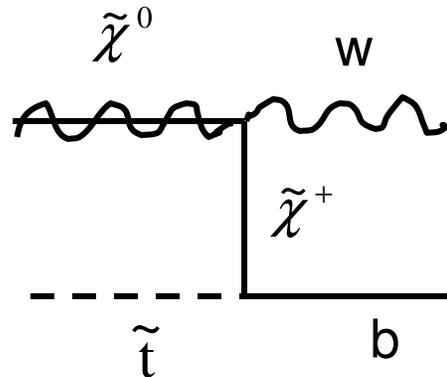
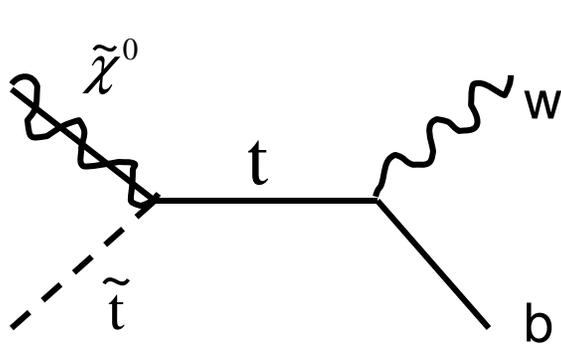
- Weakly interacting particles (WIMPS), with masses and interaction cross sections of order of the electroweak scale
→ most compelling alternative
- Supersymmetry, with R parity conservation
naturally provides a stable, neutral, dark matter candidate: $\tilde{\chi}^0$

Relic density is inversely proportional to the thermally averaged

$\tilde{\chi}^0 \tilde{\chi}^0$ annihilation cross section $\langle \sigma v \rangle$



If any other SUSY particle has mass close to the neutralino LSP, it may substantially affect the relic density via co-annihilation



if stops NLSP
neutralino-stop
co-annihilation

Conclusions

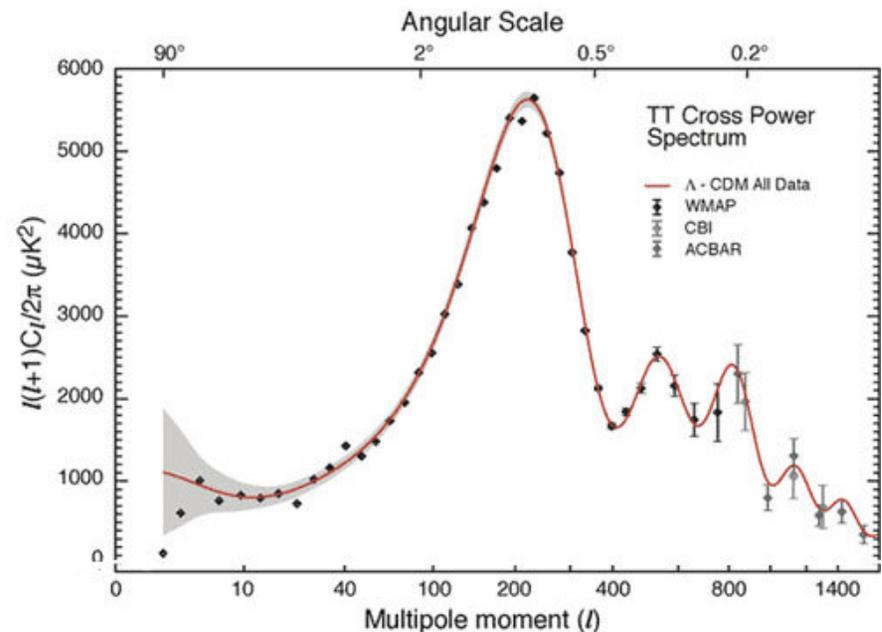
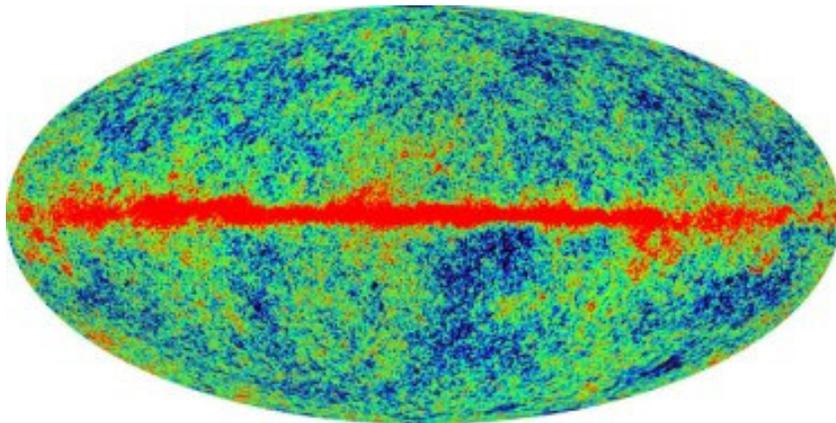
- **Supersymmetry** may play a relevant role in the origin of particle masses, is consistent with unification and provides a dark matter candidate.
- It may also be essential in the generation of the baryon asymmetry if
$$m_H < 120 \text{ GeV} \quad \text{and} \quad m_{\text{stop}} < m_{\text{top}}$$
- **Tevatron and LHC** colliders will probe soon the realization of this scenario.

Cosmic Microwave Background

WMAP measures the **CMB** and studies correlations at very small scales.
In agreement with Sloan Digital Sky Survey determined :

$$\Omega_M h^2 = 0.135 \pm 0.009 \quad \Omega_B h^2 = 0.0224 \pm 0.0009 \quad h = 0.71 \pm 0.04$$

difference gives CDM energy density: $\Omega_{\text{CDM}} h^2 = 0.1126 \pm_{0.0181}^{0.0161}$



Possible origin of Dark Matter

- Weakly interacting particles (WIMPS), with masses and interaction cross sections of order of the electroweak scale
→ most compelling alternative
- Supersymmetry, with R parity conservation naturally provides a stable, neutral, dark matter candidate: $\tilde{\chi}^0$

Relic Density

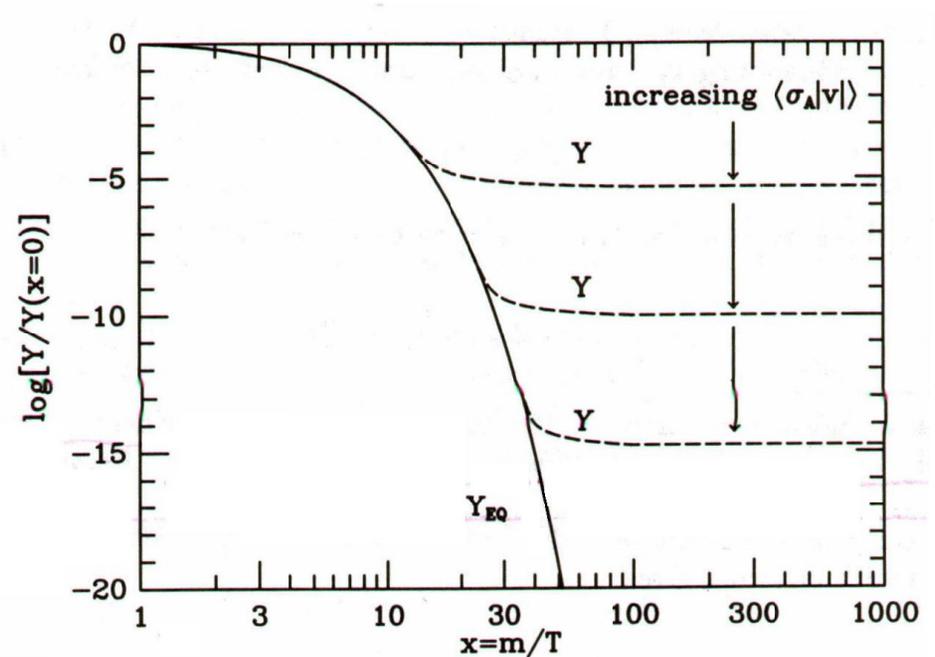
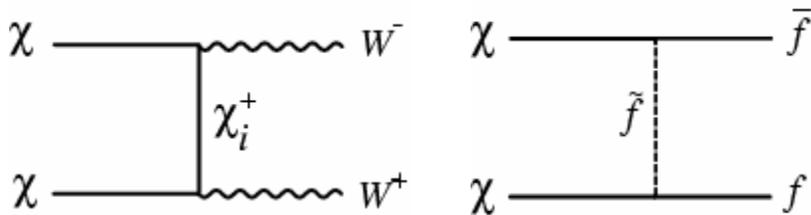
- To estimate $\tilde{\chi}^0$ relic density, assume it was in thermal equilibrium in the early universe:
$$n_{eq} = g \left(\frac{mT}{2\pi} \right)^{3/2} \text{Exp}[-m/T]$$
- Interactions with the relativistic plasma are efficient, but the WIMPs follow a Maxwell-Boltzmann distribution.
However, the universe is expanding, and once the density is small enough, they can no longer interact with one another, and fall out of equilibrium.

- Below the freeze-out temperature, the WIMPs density per co-moving volume is fixed

$$\frac{dY}{dx} = - \frac{\langle \sigma v \rangle}{H x} s (Y^2 - Y_{\text{eq}}^2) \quad \text{with } Y = n/s \text{ and } x = m/T$$

The key ingredient is the thermally averaged annihilation cross section $\langle \sigma v \rangle$

- Computing $\tilde{\chi}^0 \tilde{\chi}^0$ annihilation cross section yields the dark matter relic density



If any other SUSY particle has mass close to the neutralino LSP, it may substantially affect the relic density via co-annihilation

In Supersymmetry both problems can be solved

- EW Baryogenesis requires **new boson degrees of freedom** with strong couplings to the Higgs.
- Relevant SUSY particle: **Two Superpartners of the top, one for each chirality (left and right).**

Each stop has six degrees of freedom (3 of color, 2 of charge) and coupling of order one to the Higgs

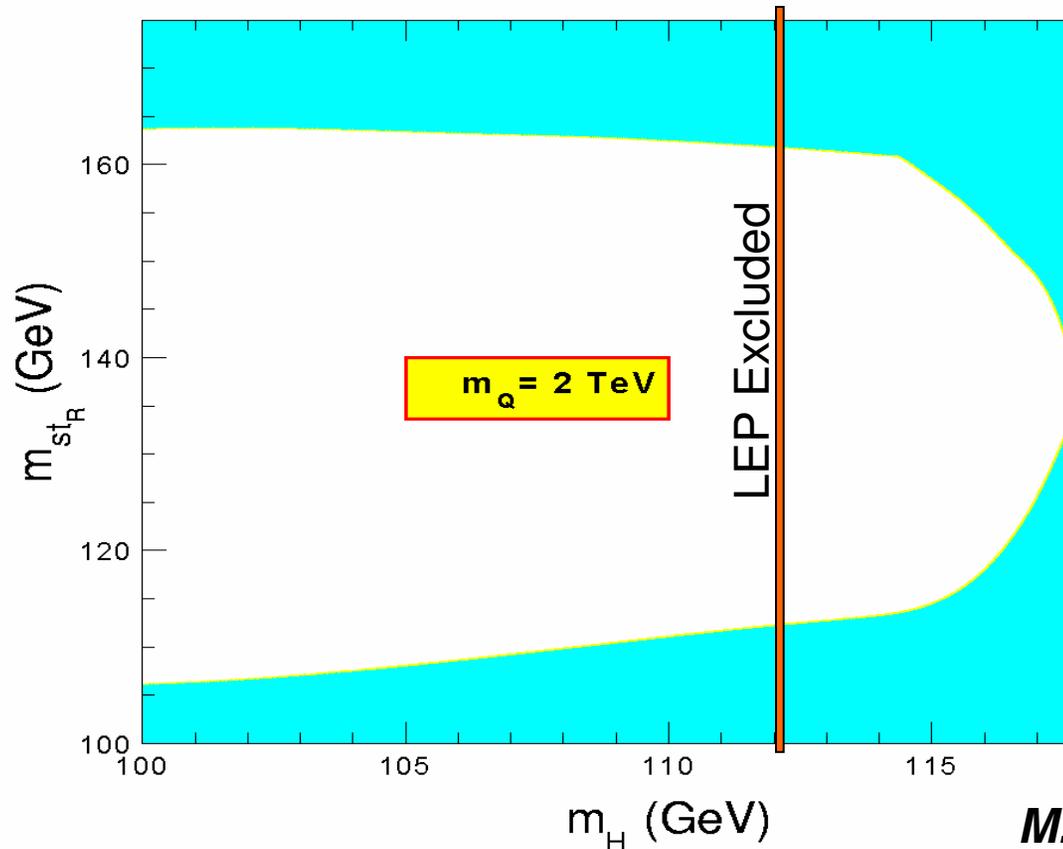
$$E_{SUSY} = \frac{g_w^3}{4\pi} + \frac{h_t^3}{2\pi} \approx 8 E_{SM} \quad \text{since} \quad \frac{v(T_c)}{T_c} \approx \frac{E}{\lambda}, \quad \text{with} \quad \lambda \propto \frac{m_H^2}{v^2}$$

One of the stops has to be light, to induce a strong first order phase transition. The other needs to be heavier than about 1 TeV in order to make the Higgs mass larger than the current bound

Upper bound on the Higgs imposed by the requirement of the preservation of the baryon asymmetry.

Limits on the Stop and Higgs Masses to preserve the baryon asymmetry

- Higgs masses up to 120 GeV may be accommodated
- The lightest stop must have a mass below the top quark mass.

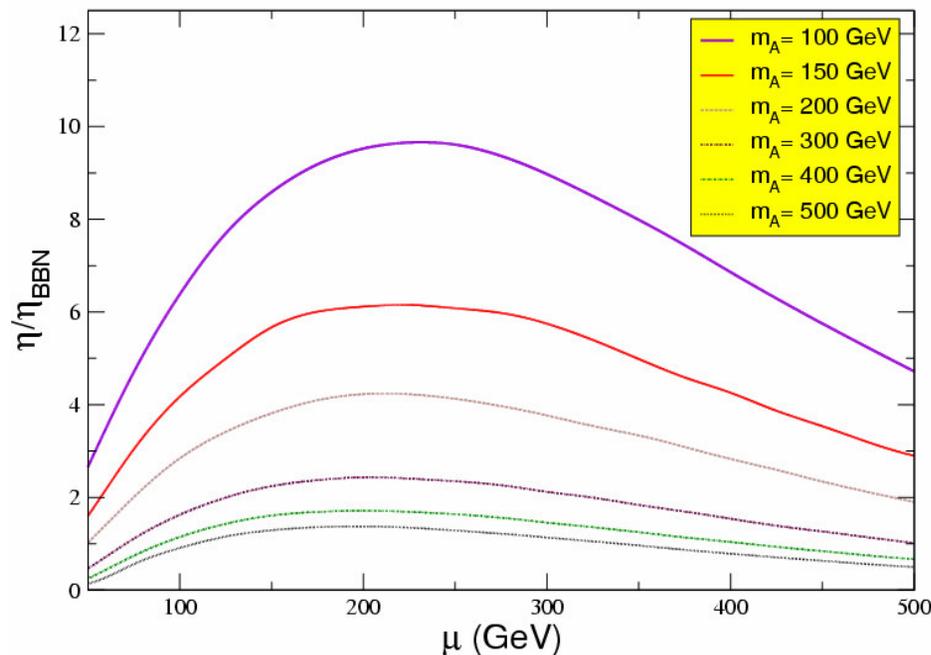


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Generation of the Baryon Asymmetry

- Superpartners of the Higgs and SU(2) gauge boson, with masses μ and M_2 (charginos), play most relevant role.
- **Baryon charge** generated in walls of bubbles expanding at the time of the first order electroweak phase transition.
- CP-violating Sources depend on $\arg(\mu^* M_2)$
- also on the bubble wall Higgs profile.
- Higgs profile depends on the mass of the heavy Higgs bosons m_A .

- New sources of CP violation from the sfermion sector
- Generation of the baryon asymmetry: Charginos with masses μ and M_2 play most relevant role.
- CP-violating Sources depend on $\arg(\mu^* M_2)$
- Higgs profile depends on the mass of the heavy Higgs bosons $M_2 = \mu$



We plot for maximal mixing:
within uncertainties, values of
 $\sin \phi_\mu \leq 0.05$ preferred

Gaugino and Higgsino masses of the order of the weak scale highly preferred

Large CP-odd Higgs mass values are acceptable

Generation Process

- Interaction with Higgs background creates a net chargino excess through CP-violating interactions
- Chargino interaction with plasma creates an excess of left-handed anti-baryons (right-handed baryons).
- Left-handed baryon asymmetry partially converted to lepton asymmetry via anomalous processes
- Remaining baryon asymmetry diffuses into broken phase
- Diffusion equations describing these processes derived

Relevant masses and Phases

- The chargino mass matrix contains new CP violating phases

$$\begin{pmatrix} M_2 & \sqrt{2}m_W \cos \beta \\ \sqrt{2}m_W \sin \beta & \mu \end{pmatrix}$$

- Some of the phases may be absorbed in field redefinition. For real Higgs v.e.v.'s, the phase

$$\arg(\mu^* M_2)$$

is physical

- Sources depend on the Higgs profile. They vanish for large values of

$$\tan \beta = \frac{v_2}{v_1}$$

Upper Bound on the Lightest Higgs Mass (minimal SUSY)

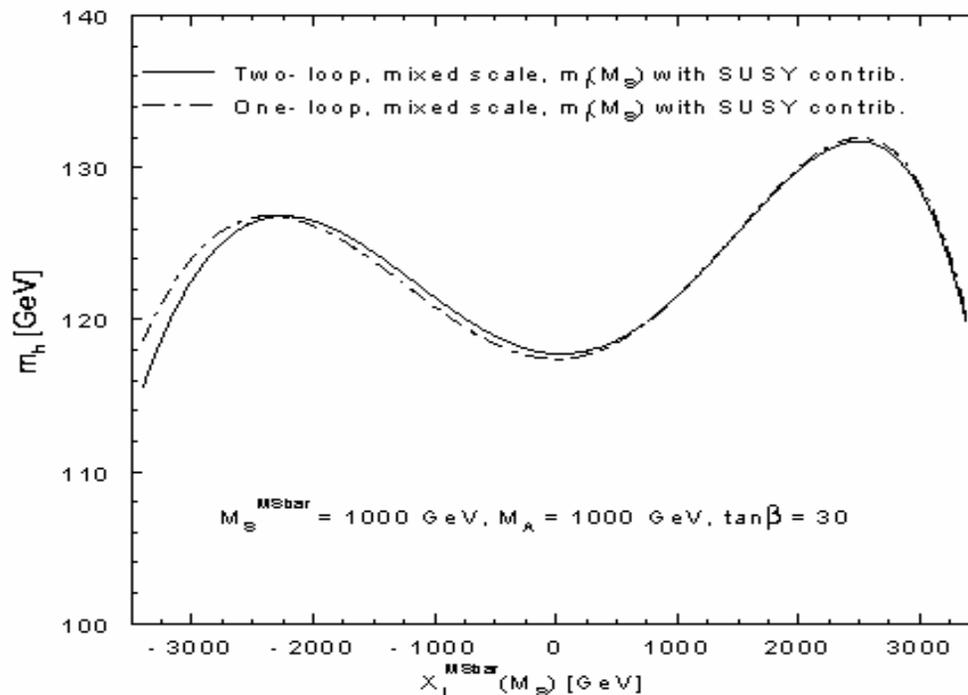
Supersymmetry requires two Higgs doublets. Two CP-even and one CP-odd neutral Higgs bosons.

$$\langle H_2 \rangle = v_2 \quad , \quad \langle H_1 \rangle = v_1$$

M_S = Mass of the top-quark superpartner

M_A = Mass of the heavy neutral Higgs bosons

X_t = Left-right Stop mixing parameter

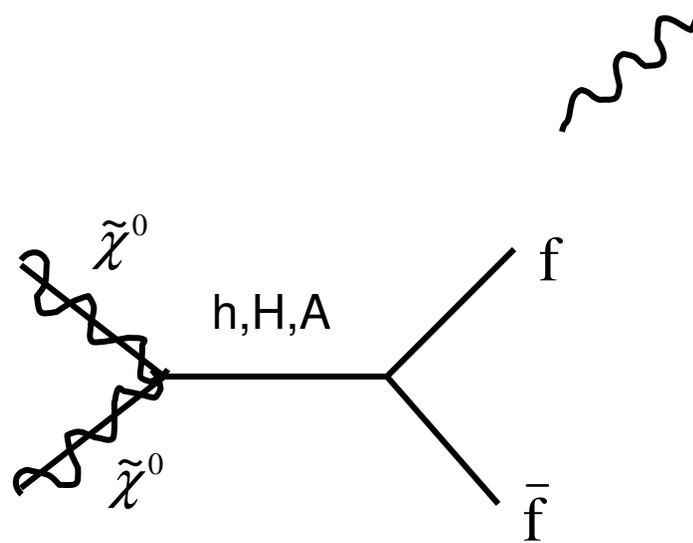
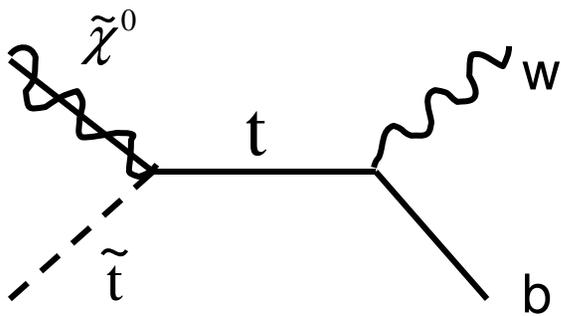


**Lightest Higgs boson
mass smaller than
135 GeV.**

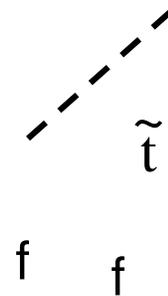
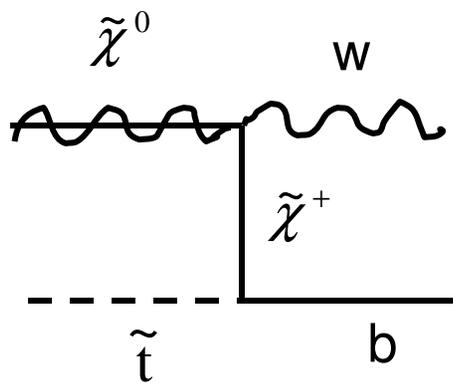
M. Carena, M. Quiros, C.W. (1996); with Haber et al. (2000)

Stop Signatures

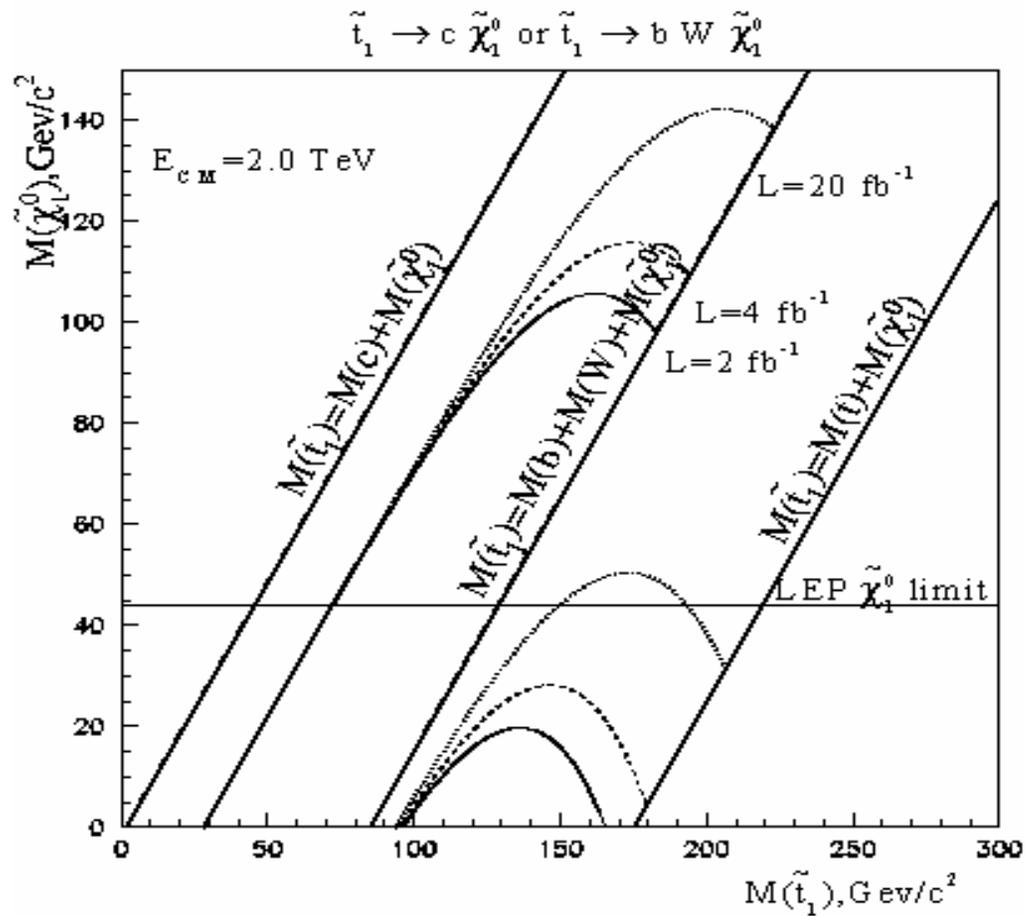
- Light Stop can decay into the lighter charginos or neutralinos.
- Stop signatures depend on this and also on the mechanism of supersymmetry breaking.
- In standard scenarios, where neutralino is the dark matter, stop may decay into a light up-quark and a neutralino: Two jets and missing energy.
- In models in which supersymmetry is broken at low energies, the neutralino may decay into a photon and a gravitino, the superpartner of the graviton.



$m_A = 2 m_{\tilde{\chi}}$ the $\tilde{t} - \tilde{\chi}$

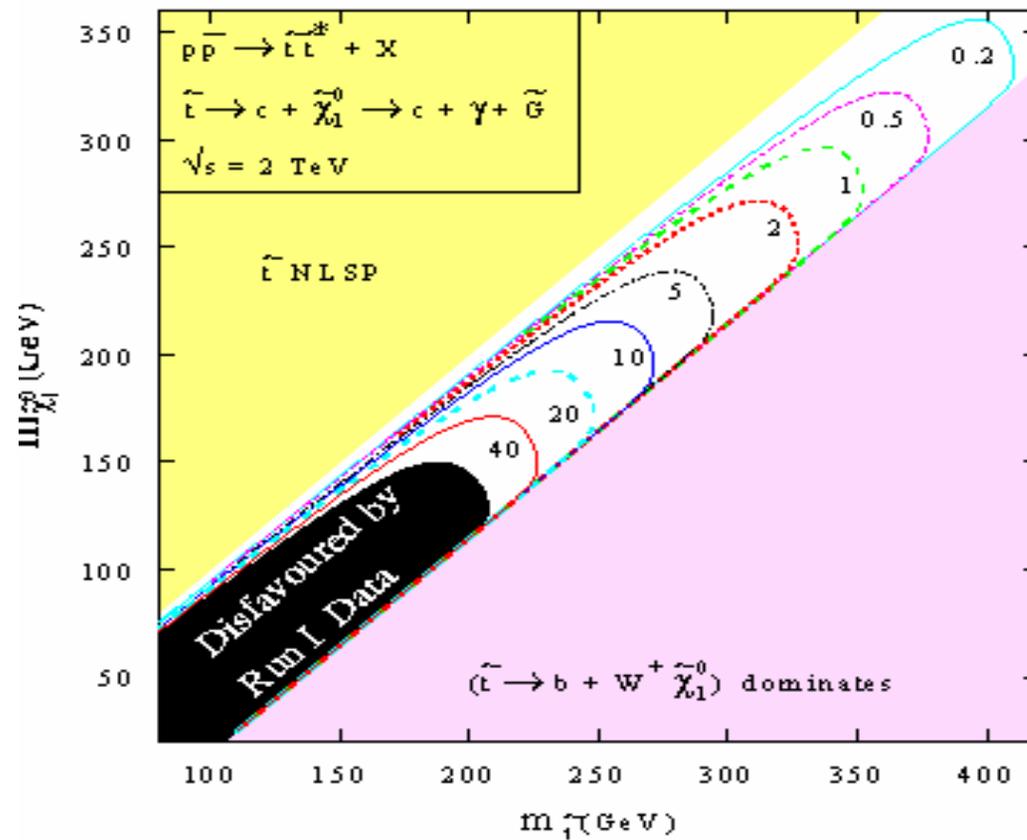


Stop Signatures at the Tevatron Neutralino as Dark Matter



Stop Searches at the Tevatron

Neutralino decaying into photons



Washout of Baryon Asymmetry

- *Baryon Number violated in the SM at high temperatures.*
- B-L, instead, is preserved by anomalous processes

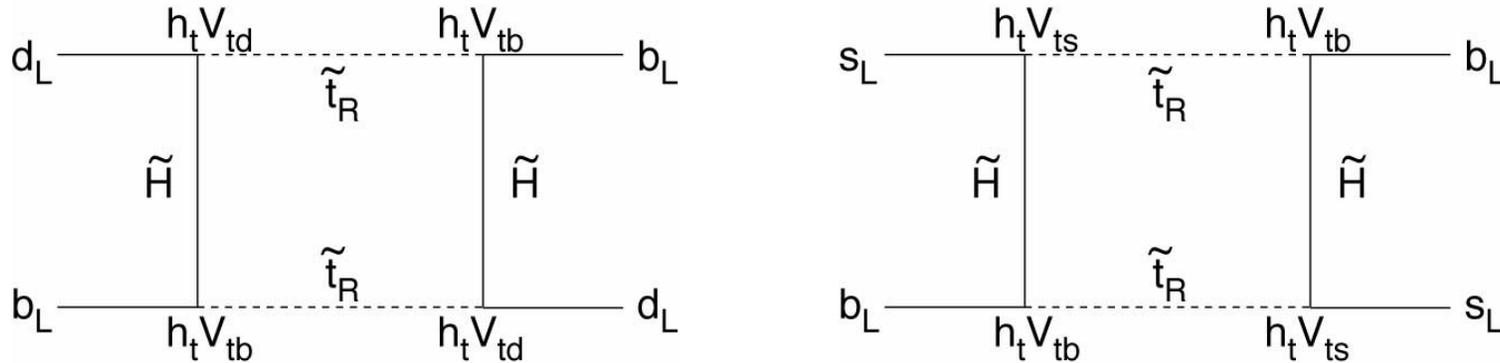
$$\Delta B = \Delta L = N_g \Rightarrow \Delta(B-L) = 0$$

- If, original asymmetry had $B = L$, final asymmetry : $B = L = 0$.
- For successful generation of B asymmetry, decay of heavy particles should lead to

$$B-L \neq 0$$

Other Signals

- **20% enhancements** to Δm_d , Δm_s with the same phase as in the SM (Murayama, Pierce)



- Large phases in the chargino sector may induce large electric dipole moments for quarks and leptons: They lead to a bound on the first and second generation sfermions masses of about 2 TeV (Pilaftsis, Carena, Quiros, Seco and C.W.)

Why Supersymmetry ?

- Helps to stabilize the weak scale—Planck scale hierarchy
- Supersymmetry algebra contains the generator of space-time translations.
Necessary ingredient of theory of quantum gravity.
- Minimal supersymmetric extension of the SM :
Leads to Unification of gauge couplings.
- Starting from positive masses at high energies, electroweak symmetry breaking is induced radiatively.
- If discrete symmetry, $P = (-1)^{3B+L+2S}$ is imposed, lightest SUSY particle neutral and stable: Excellent candidate for cold Dark Matter.

Problems in the Standard Model

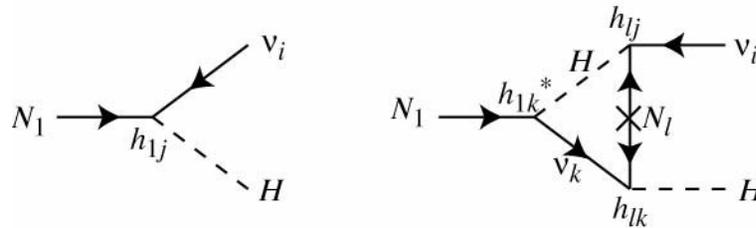
- A more careful examination shows that, in the SM, phase transition is a cross over for any value of the Higgs mass.
- Second, independent problem: Not enough CP violation. In the SM, this is measured by

$$\det[M_u^+ M_u, M_d^+ M_d] / T_c^{12} \approx 10^{-20}$$

- Both problems solved with **Supersymmetry**:
Phase Transition strongly first order
New CP violating phases

Leptogenesis

- Heavy, right-handed neutrinos decay out-of-equilibrium



- CP violating phases appear in the interference between the tree-level and one-loop amplitudes.
- Majorana fermions have extra physical phases. Two generations of neutrinos would be sufficient for the mechanism to work
- *Detailed calculation shows that lightest right handed neutrino mass should be $M_1 \sim 10^{10}$ GeV to obtain proper baryon asymmetry.*
- Leptogenesis may work even in the absence of supersymmetry. (In SUSY reheating temperatures of the order of dangerous, since they lead to overproduction of gravitinos).

Higgs Physics and Supersymmetry

- Quartic couplings of the Higgs boson governed by the gauge couplings.
- At tree level, the lightest Higgs boson mass is smaller than M_Z (91 GeV).
- Prediction modified by radiative corrections induced by **supersymmetry breaking** effects.
- Most relevant particle : Superpartner of the top-quark (large coupling to the Higgs).

Anomalies arise in the process of regularization of divergences. Impossible to do it preserving gauge and B and L symmetries.

$$\partial^\mu j_\mu^{B,L} = \frac{N_g}{32\pi^2} \text{Tr} \left(\varepsilon^{\mu\nu\alpha\beta} F_{\mu\nu} F_{\alpha\beta} \right)$$

Instantons are minimal action configuration with non-vanishing values of the integral of the right-hand side of the above Eq.

Instanton configurations may be regarded as semiclassical amplitudes for tunnelling effect between vacuum states with different baryon number

$$S_{inst} = \frac{2\pi}{\alpha_W} \quad \Gamma_{\Delta B \neq 0} \propto \exp(-S_{inst})$$

Weak interactions: Transition amplitude exponentially small. No observable baryon number violating effects at $T = 0$

Non-equivalent Vacua and Static Energy in Field Configuration Space

Vacua carry different baryon number.

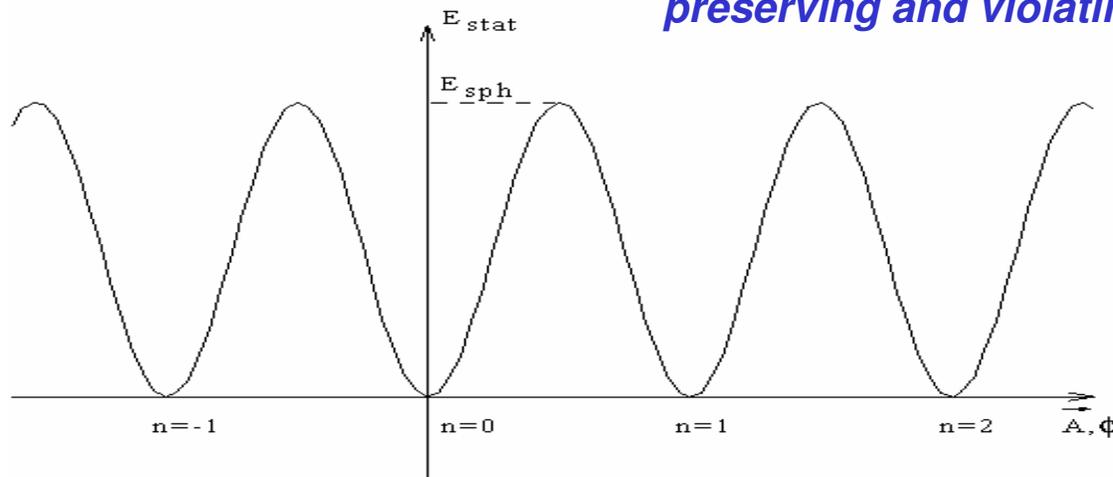
The sphaleron is a static configuration with non-vanishing values of the Higgs and gauge boson fields.

Its energy may be identified with the height of the barrier separating vacua with different baryon number

$$E_{sph} = \frac{8\pi v}{g_W}$$

The quantity v is the Higgs vacuum expectation value, $\langle H \rangle = v$.

This quantity provides an order parameter which distinguishes the electroweak symmetry preserving and violating phases.



Heavy Particle Decay with $B-L \neq 0$

- Idea : Generate a non-vanishing lepton number at high energies.
- Baryon number generated from lepton number plus anomaly interactions, which convert L to B: **Leptogenesis** (Fukugita, Yanagida)
- Makes use of standard explanation of small neutrino masses.
- Relies in the presence of heavy Majorana neutrinos
- *Detailed calculation shows that lightest right handed neutrino mass should be $M_M \sim 10^{10}$ GeV to obtain proper baryon asymmetry.*

Baryogenesis by Decay of Heavy Particles

- First simple models of baryogenesis proposed in the context of Grand Unified Models.
- A heavy GUT-scale particle X decays out-of-equilibrium with **direct CP violation**

$$B(X \rightarrow q) \neq B(\bar{X} \rightarrow \bar{q})$$

Neutrino Masses: Seesaw Mechanism

- Neutrino Masses much smaller than charged fermion ones
- Explanation: Neutrinos are Majorana particles. Dirac mass equal in size to charged particle masses.
- Large right handed mass. Mass matrix in base

$$(V_L, V_R) \quad \begin{bmatrix} 0 & m_D \\ m_D^T & M \end{bmatrix}$$

- Small mass eigenvalue, consistent with experiment if M is very large

$$m_i = \frac{m_{D_i}^2}{M_i} \quad (m = m_D M^{-1} m_D^T)$$