

# 1 Equations

$$\frac{d\sigma}{d\Omega_Z d\Omega_l} = \sum_{\lambda_{ll}\lambda_\gamma} \left| \sum_{J_{Z\gamma}\lambda_Z\lambda_{qq}} [2J_{Z\gamma} + 1] T_{\lambda_Z\lambda_\gamma\lambda_{qq}}^{J_{Z\gamma}} d_{\lambda_Z\lambda_\gamma\lambda_{qq}}^{J_{Z\gamma}}(\cos\theta_Z) \right. \\ \left. \otimes A_{\lambda_Z\lambda_{ll}} d_{\lambda_Z\lambda_{ll}}^1(\cos\theta_l) e^{i[\lambda_{qq}\phi_Z - \lambda_Z(\phi_Z + \phi_l)]} \right|^2 \quad (1)$$

Equation (1) is described by *fitFunc()*, but in order to construct  $-\ln L$ , where  $L$  is the likelihood it has to be brought to the form:

$$W(\Omega) = \sum_n^{N_{par}} A_n \omega_n(\Omega) \quad (2)$$

For squaring following formulas are used:

If  $a_i$  and  $\alpha_i$  are real:

$$\left| \sum_i a_i e^{i\alpha_i \phi_i} \right|^2 = \sum_i \sum_{j \geq i} (2 - \delta_{ij}) a_i a_j \cos(\alpha_i \phi_i - \alpha_j \phi_j)$$

in general, helicity amplitudes are complex numbers, so, if  $z_i = a_i + ib_i$  and let's also put some  $x_i$  real functions in general calculation (which represent the wigner  $d$  functions in our distribution):

$$\left| \sum_i z_i x_i e^{i\alpha_i \phi_i} \right|^2 = \sum_i \sum_{j \geq i} (2 - \delta_{ij}) x_i x_j (a_i a_j + b_i b_j) \cos(\alpha_i \phi_i - \alpha_j \phi_j)$$

Which results in

$$\frac{n(n+1)}{2}$$

members of summation.

Finally we get:

$$W(\Omega) = \sum_n^{N_{par}} A_n \omega_n(\Omega) = \sum_{\lambda_\gamma \lambda_{ll}} \sum_i \sum_{j \geq i} (2 - \delta_{ij}) x_i x_j (a_i a_j + b_i b_j) \cos(\alpha_i \phi_i - \alpha_j \phi_j)$$

But, this is a lot of members of summation, whereas we have less independent amplitudes, 9 for  $A_{\lambda_Z\lambda_{ll}}$  and 32 for  $T_{\lambda_Z\lambda_\gamma\lambda_{qq}}^J$ .